

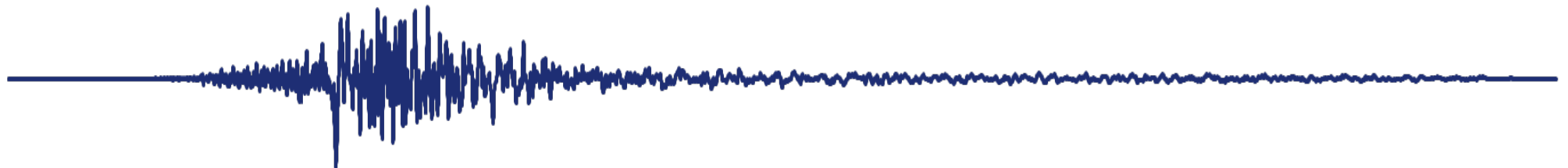
Vancouver Geotechnical Society

NBC 2020- Compatible Seismic Site Response Analysis Approach

Chris Weech, M.A.Sc., P.Eng.
November 16, 2022

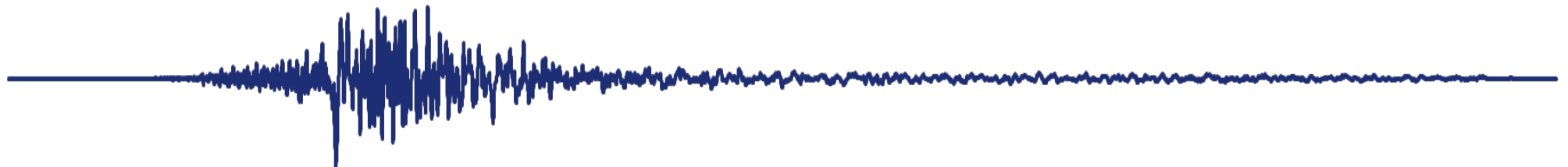


Christchurch, NZ (Feb. 22, 2011)



Presentation Outline

- Aggregated hazard from seismic hazard calculator vs event scenario hazard as examined from deaggregation data
- Differences in site amplification treatment in the 6th Generation Seismic Hazard Model of Canada (SHMC-6) adopted by NBC 2020 compared to NBC 2015:
 - NBC 2015 – Non-linear amplification according to aggregated probabilistic PGA_{ref}
 - SHMC-6 – Non-linear amplification according to event scenario median ground motion intensity
- Probabilistic distribution of event scenario hazard values from NBC 2020 deaggregation data
- Current practice for Seismic Site Response Analyses (SSRA) based on NBC 2015 aggregated hazard values
- Study demonstrating implementation of SSRA results within SHMC-6 compared to simplified methods of calculating NBC 2020-compatible Uniform Hazard Response Spectra (UHRS) using SSRA results



Probabilistic Seismic Hazard Values

<https://www.earthquakescanada.nrcan.gc.ca/hazard-alea/interpolat/calc-en.php>

Site: 48.4191 N, 123.3703 W User File Reference: Legislative Assembly of BC, Victoria, BC

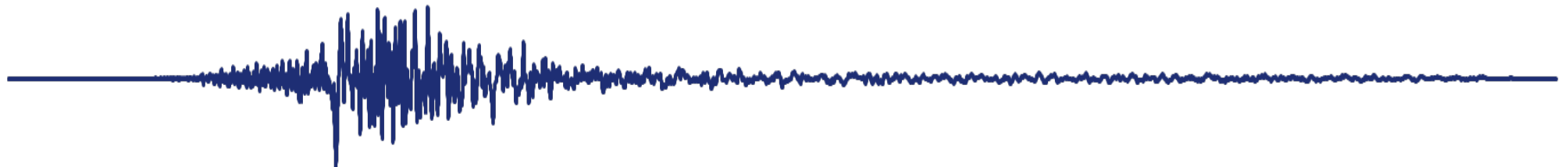
Requested by: ,

National Building Code ground motions: 2% probability of exceedance in 50 years (0.000404 per annum) ↙ 1 / 2,475 years

Uniform
Hazard
Response
Spectrum
(UHRS)

Sa(0.05)	Sa(0.1)	Sa(0.2)	Sa(0.3)	Sa(0.5)	Sa(1.0)	Sa(2.0)	Sa(5.0)	Sa(10.0)	PGA (g)	PGV (m/s)
0.709	1.082	1.300	1.301	1.154	0.674	0.397	0.124	0.043	0.579	0.830

Notes. Spectral ($S_a(T)$, where T is the period in seconds) and peak ground acceleration (PGA) values are given in units of g (9.81 m/s^2). Peak ground velocity is given in m/s . Values are for "firm ground" (NBCC 2015 Site Class C, average shear wave velocity 450 m/s). NBCC2015 and CSAS6-14 values are specified in **bold font**. Three additional periods are provided - their use is discussed in the NBCC2015 Commentary. Only 2 significant figures are to be used. *These values have been interpolated from a 10-km-spaced grid of points. Depending on the gradient of the nearby points, values at this location calculated directly from the hazard program may vary. More than 95 percent of interpolated values are within 2 percent of the directly calculated values.*



Aggregated Probabilistic Seismic Hazard

- Probabilistic Hazard Values referenced to Probability of Exceedance in 50 yrs (PoE_{50}) or Annual Exceedance Rate (AER):

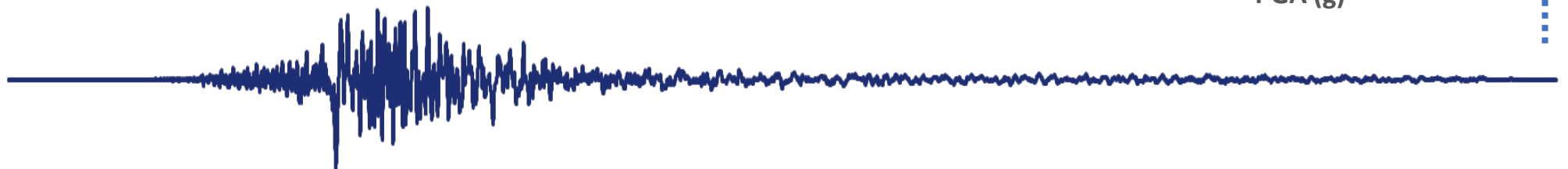
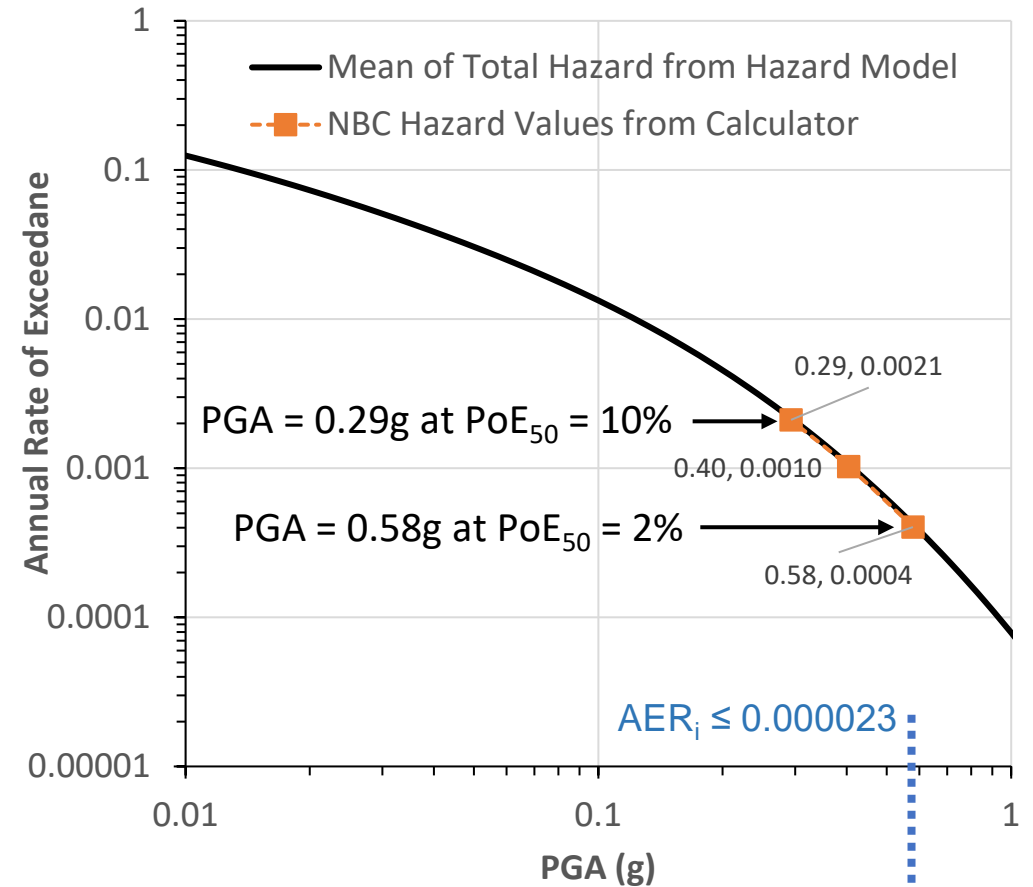
$$1 - PoE_{50} = (1 - AER)^{50}$$

- “Return Period” = $1/AER$ – not to be confused with the Average Recurrence Period of the EQ event
- Probabilistic Hazard Value at a specified AER obtained from a “Hazard Curve”

eg. $PGA(AER = 0.000404) = 0.58g$

- Total Hazard: $AER_{TH}(X) = \sum AER_i(X, M_i, R_i)$, where
 X = probabilistic hazard value (eg. PGA)
 M_i = earthquake magnitude of event scenario i
 R_i = source-site distance of event scenario i

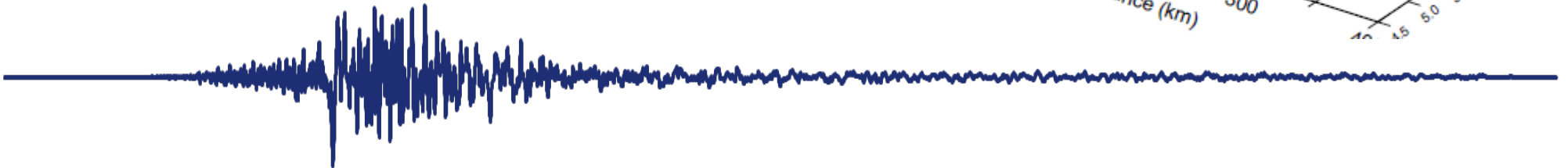
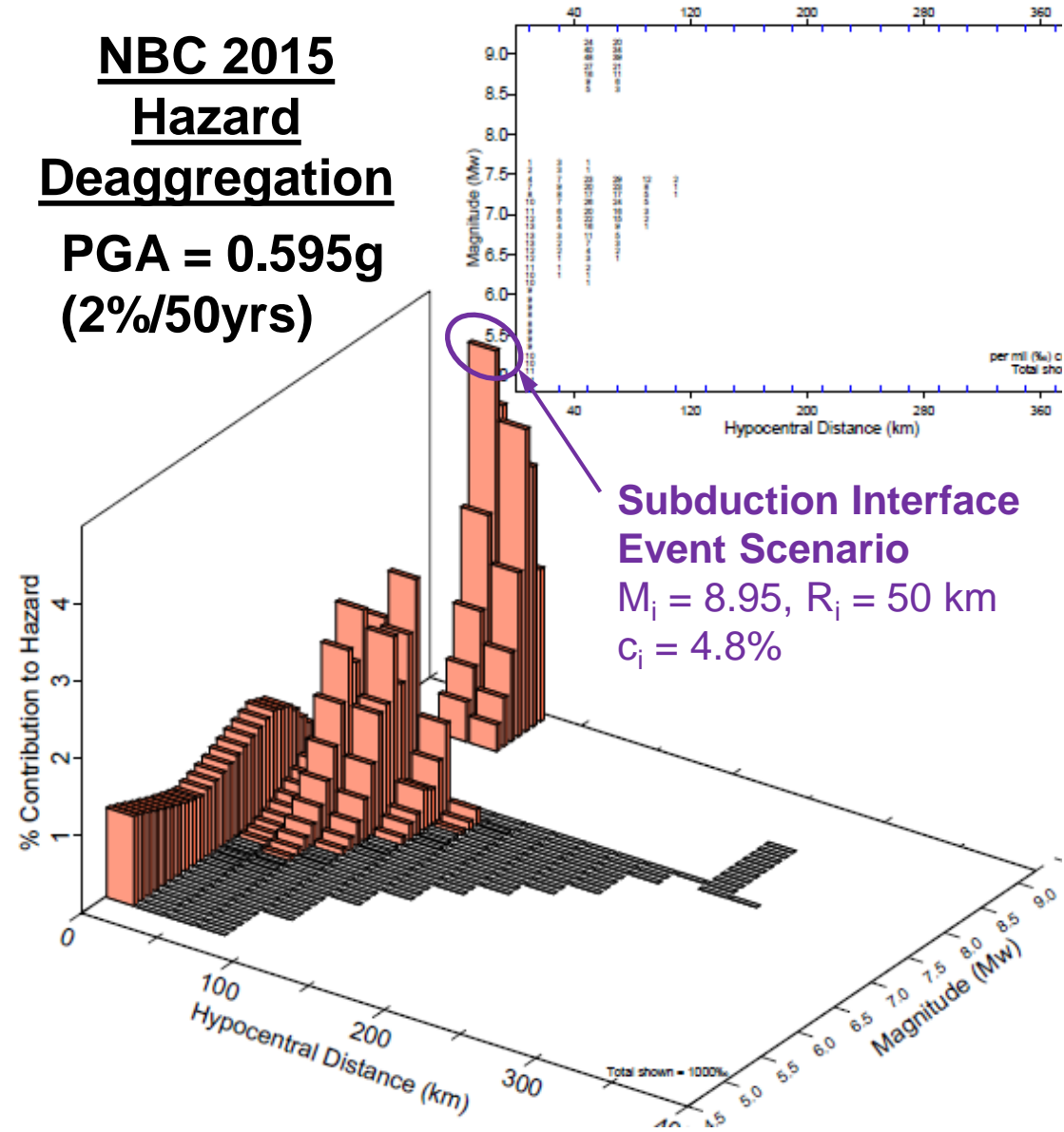
Aggregated Hazard Curve
 PGA for $Vs30 = 1100$ m/s in Victoria



Deaggregated Hazard

- Deaggregation data indicates % contributions of individual event scenarios to total hazard value (X) at specified AER_{TH} :
 - Event scenario contribution, $c_i = AER_i / AER_{TH}$
- Deaggregation data provides c_i for each M_i, R_i “bin”
- NBC 2015 does not reveal predicted PGA_i
- Example:
 - $PGA = 0.595g, AER_{TH} = 0.0404\%$ p.a. (NBC 2015)
 - Modal $M_i = 8.95, R_i = 50$ km, $c_i = 4.8\%$
 - $AER_i = c_i \cdot AER_T = 0.0019\%$ ($PoE_{50} = 0.097\%$)
 - $1/AER_i = 52,000$ years

NBC 2015
Hazard
Deaggregation
PGA = 0.595g
(2%/50yrs)



Amplification in NBC 2015

- Probabilistic hazard values ($S_a(T)$, PGA, PGV) for Site Class C reference ground condition generated by 5th Generation Seismic Hazard Model of Canada (SHMC-5)
- Site amplification from Site Coefficient tables provided in the code: $F(T, \text{Site Class}, \text{PGA}_{\text{ref}})$:
 - PGA_{ref} is the ground motion “intensity measure” to account for non-linear amplification effects
 - $\text{PGA}_{\text{ref}} = \text{PGA}_C$, or 0.8PGA_C (if $\text{PGA}_C/S_a(T) > 0.5$)
 - PGA_C is the probabilistic PGA (for Site Class C) at the design hazard level
- Site Class-specific amplified hazard values: $S(T, \text{SC}) = S_a(T) \cdot F(T, \text{SC}, \text{PGA}_{\text{ref}})$

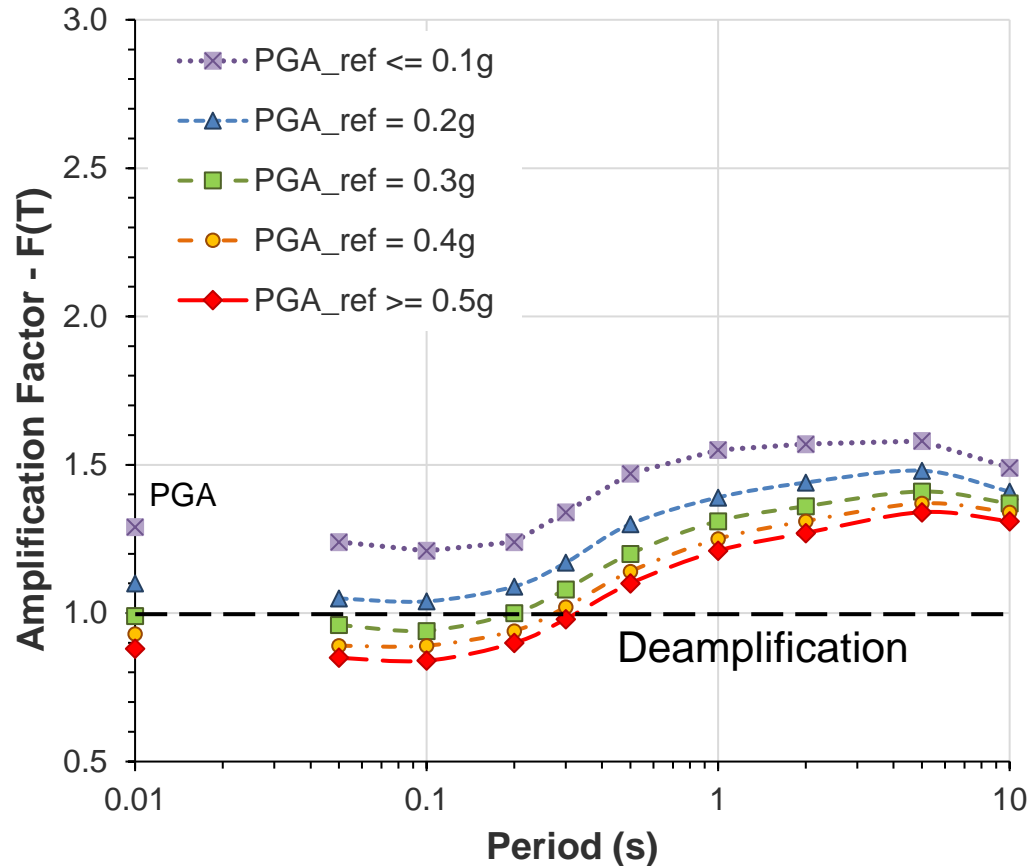
Table 4.1.8.4.-B
 Values of $F(0.2)$ as a Function of Site Class and PGA_{ref}
 Forming Part of Sentences 4.1.8.4.(4) and (5)

Site Class	Values of $F(0.2)$				
	$\text{PGA}_{\text{ref}} \leq 0.1$	$\text{PGA}_{\text{ref}} = 0.2$	$\text{PGA}_{\text{ref}} = 0.3$	$\text{PGA}_{\text{ref}} = 0.4$	$\text{PGA}_{\text{ref}} \geq 0.5$
A	0.69	0.69	0.69	0.69	0.69
B	0.77	0.77	0.77	0.77	0.77
C	1.00	1.00	1.00	1.00	1.00
D	1.24	1.09	1.00	0.94	0.90
E	1.64	1.24	1.05	0.93	0.85
F	(1)	(1)	(1)	(1)	(1)

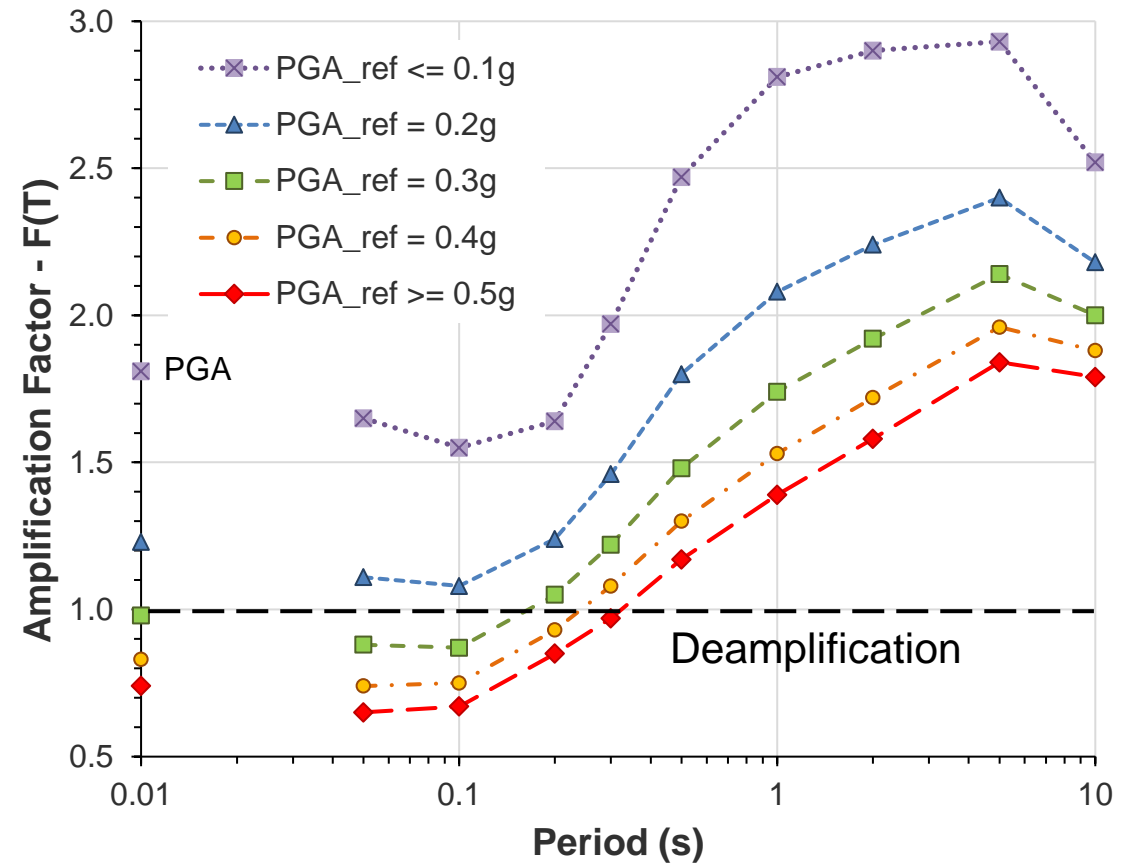


NBC 2015 Site Coefficients – $F(T, PGA_{ref})$

Site Class D ($V_{s30} = 250$ m/s)



Site Class E ($V_{s30} = 115$ m/s)

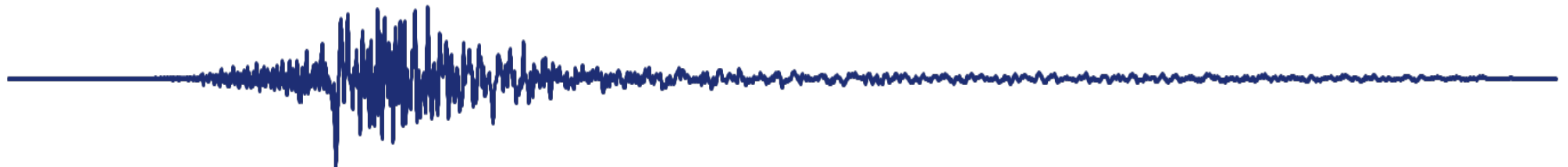


Amplification in NBC 2020

- Amplification of rock ground motion values associated with individual event scenarios are calculated internally within SHMC-6 using multiple Ground Motion Models (GMMs) specific to each tectonic regime
- For each empirical GMM:
 - a site term based on V_{s30} is used to calculate linear (elastic) amplification
 - a site term based on the median prediction of (typ.) PGA_{rock} for individual event scenarios is used to calculate non-linear effects
- The amplified hazard values are probabilistically aggregated to generate Uniform Hazard Response Spectra (UHRS), PGA, PGV as a function of V_{s30}

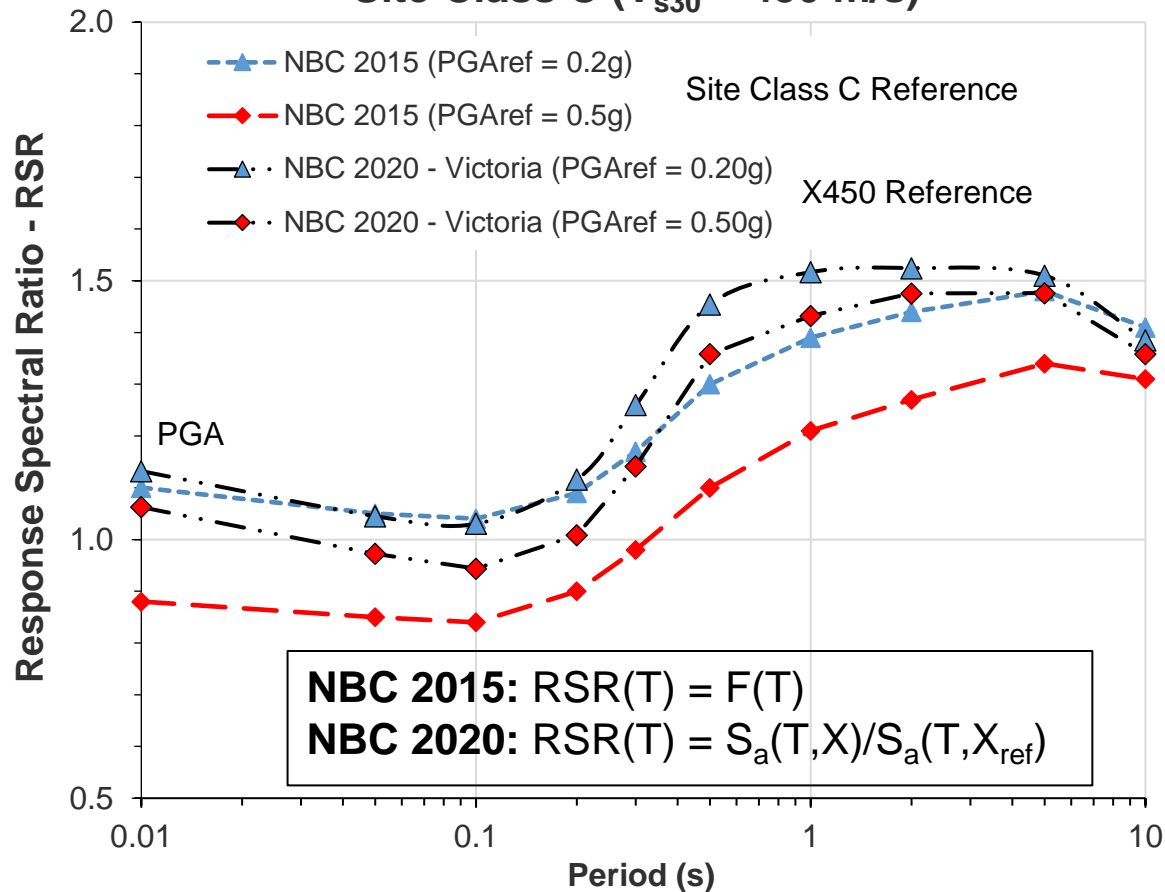
Tectonic Regime	GMM	Weight
Subduction Inslab	Aea15	0.25
	Zea06	0.25
	AB03	0.25
	Gea05	0.25
Subduction Interface	Aea15	0.25
	Zea06	0.25
	GA14	0.25
	AM09	0.25
Active Crust	ASK14	0.25
	BSSA14	0.25
	CB14	0.25
	CY14	0.25

Ref: Kolaj et al. (2019). "Ground-motion models for the 6th Generation Seismic Hazard Model of Canada"

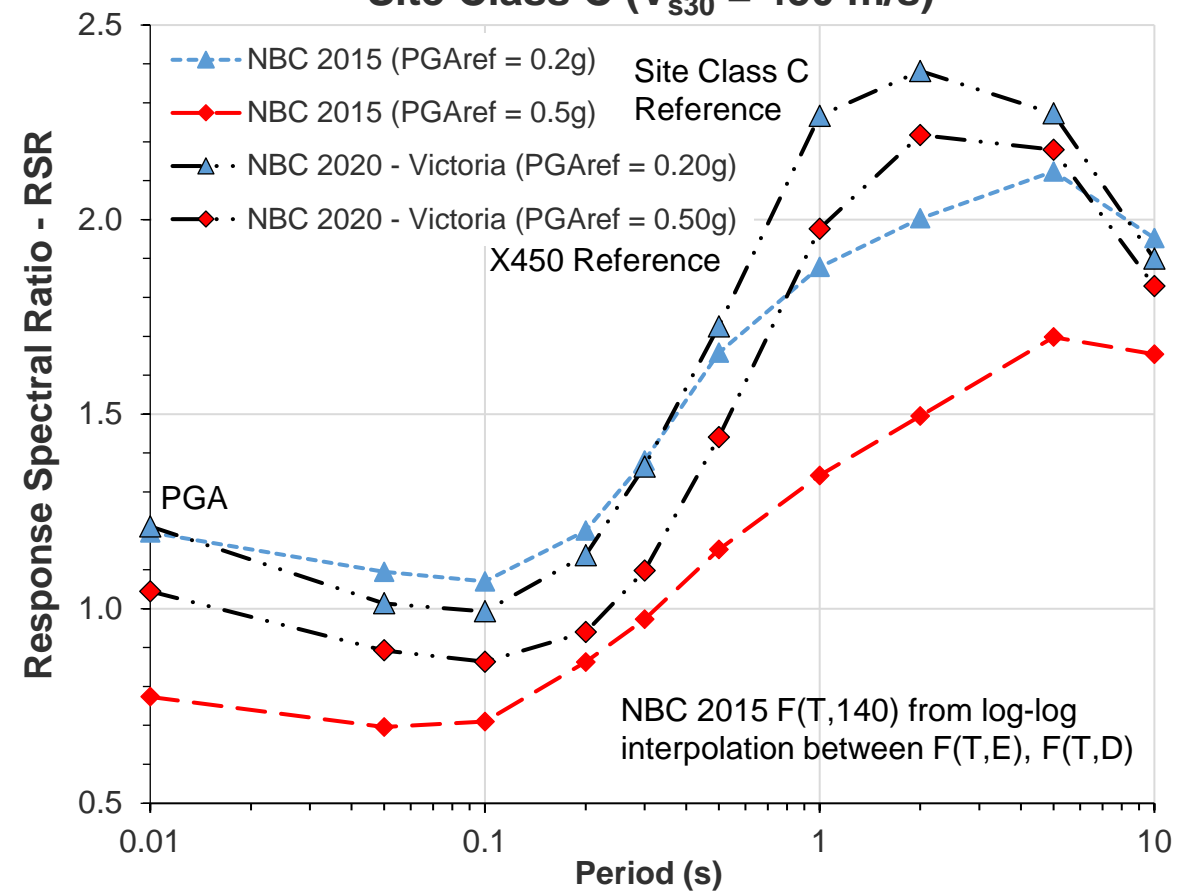


NBC 2020 vs NBC 2015 Amplification

Site Class D ($V_{s30} = 250$ m/s) relative to Site Class C ($V_{s30} = 450$ m/s)

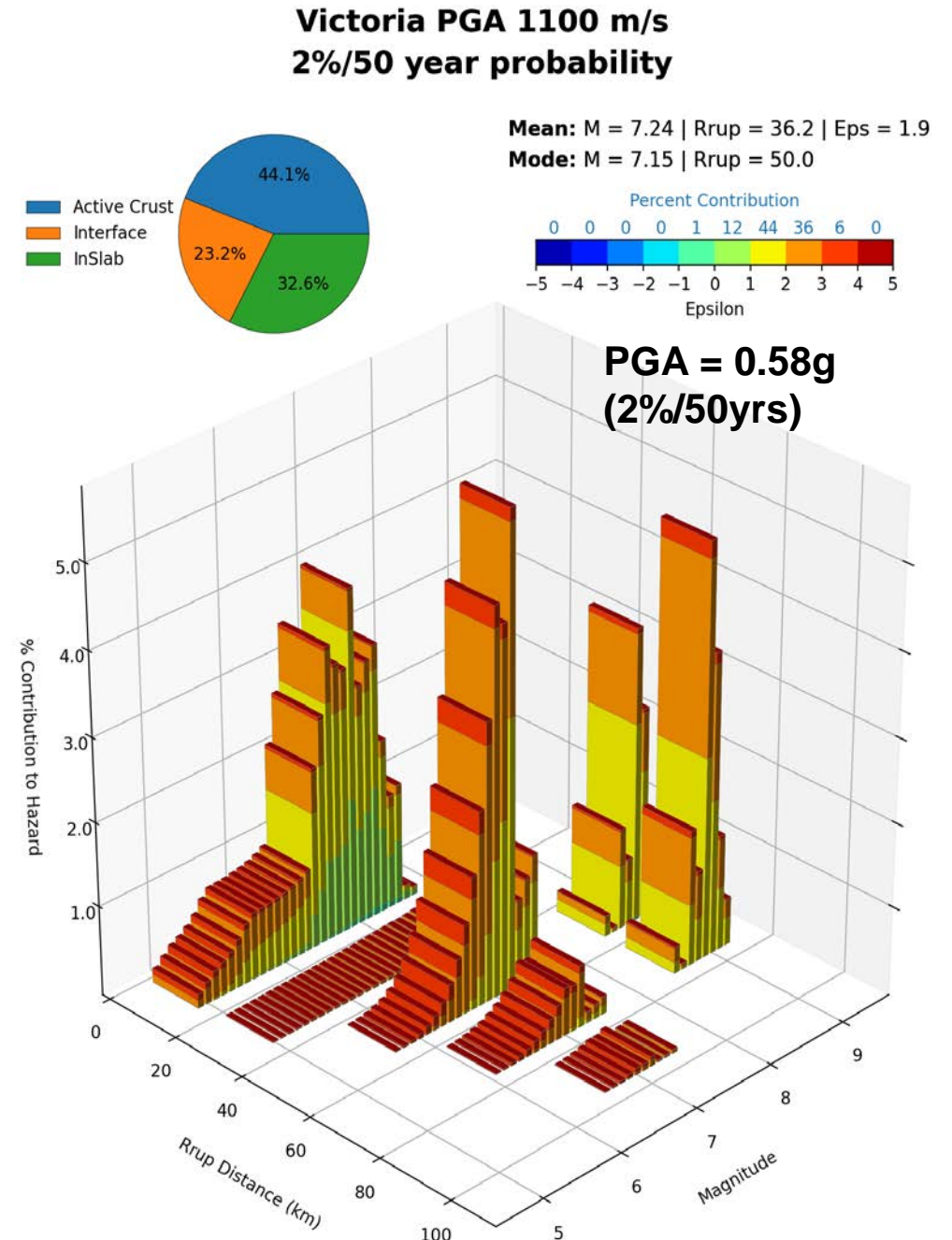
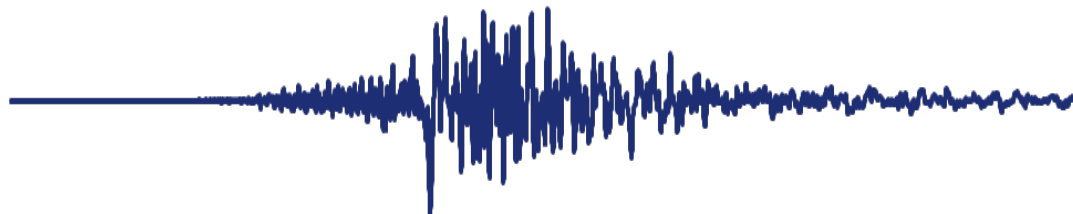


Site Class E ($V_{s30} = 140$ m/s) relative to Site Class C ($V_{s30} = 450$ m/s)



SHMC-6 Deaggregation

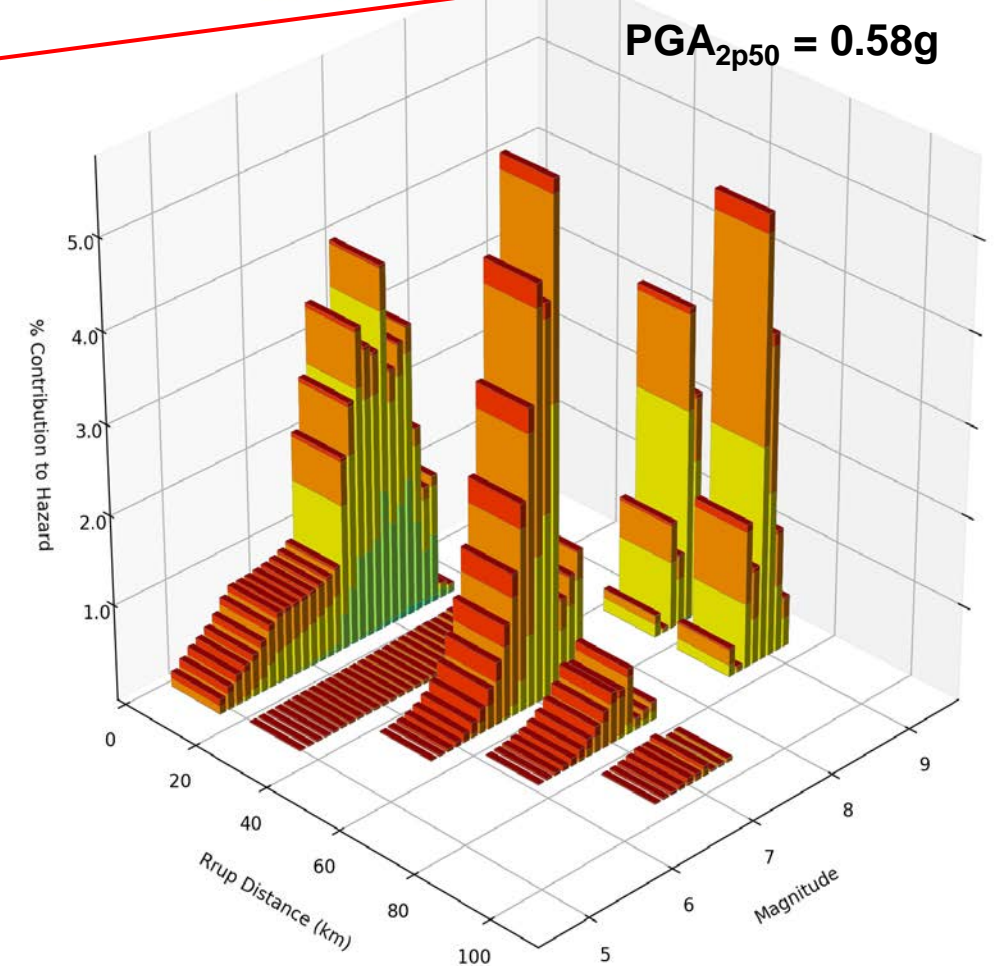
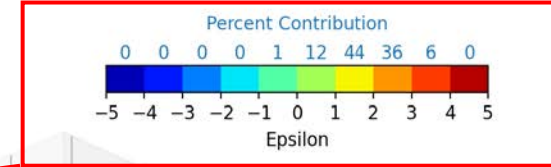
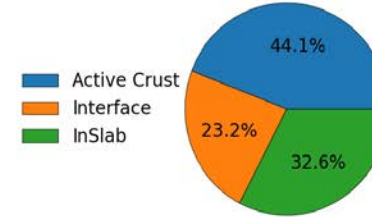
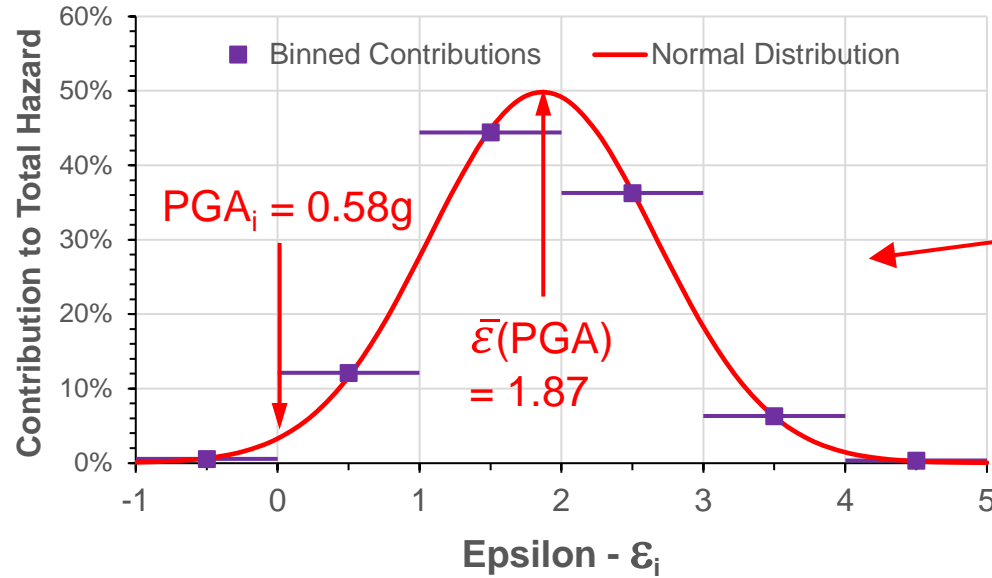
- Deaggregation data from OpenQuake provides c_i for each M_i, R_i bin which are now proportioned according to “epsilon”
- Epsilon (ε) is a measure of the number of standard deviations (in log units), σ , between the natural log of the probabilistic total hazard value at the design hazard level, $\ln(X)$, and the mean (μ_i) of $\ln(x_i)$ for event scenario i having M_i, R_i
 i.e. $\ln(X) = \mu_i + \varepsilon_i \cdot \sigma$
- $\mu_i = \ln(\text{med_}x_i)$, where $\text{med_}x_i$ is the median of the log-normal distribution of x_i – i.e. $\text{med_}x = e^\mu$
- σ is a measure of the aleatoric uncertainty in GMM’s prediction of μ_i which is attributed to event-to-event and site-to-site variability



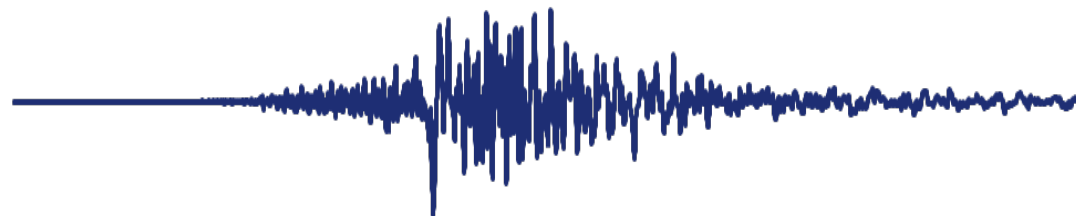
ϵ_i & $\bar{\epsilon}$ from Deaggregation

Victoria PGA 1100 m/s
2%/50 year probability

Mean: $M = 7.24$ | $R_{rup} = 36.2$ | $Eps = 1.9$
Mode: $M = 7.15$ | $R_{rup} = 50.0$



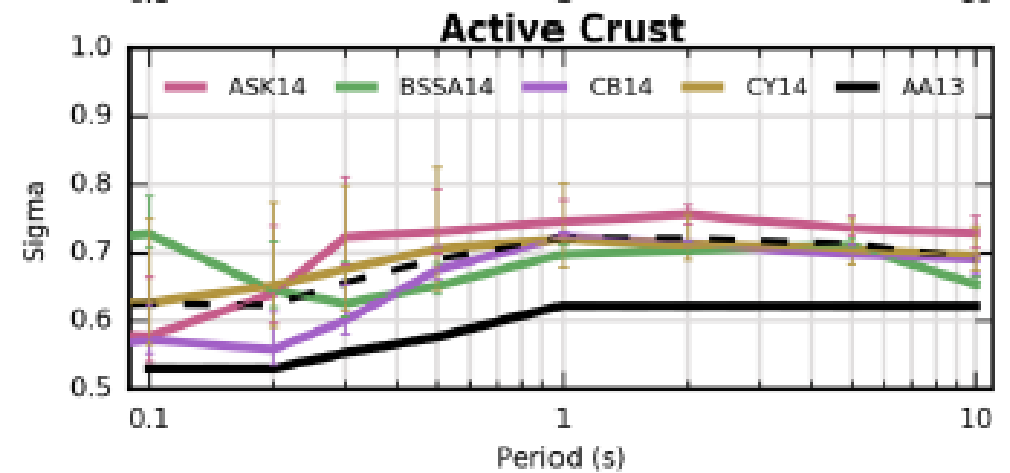
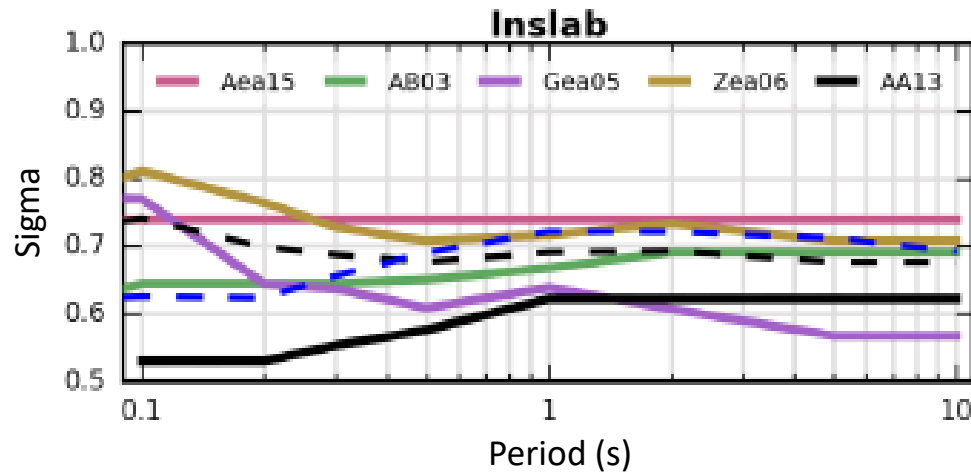
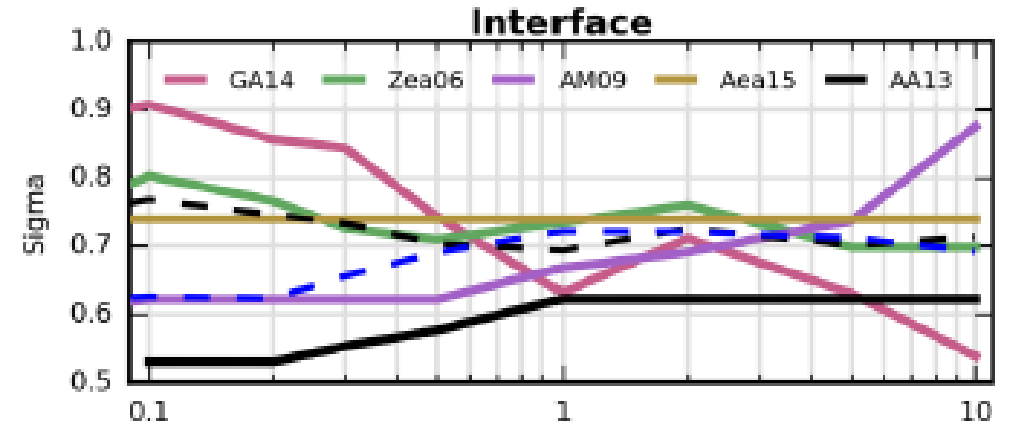
Tectonic Regime	Contribution	$\bar{\epsilon}(PGA)$
Crustal	44%	1.51
In-Slab	33%	2.29
Interface	23%	1.96



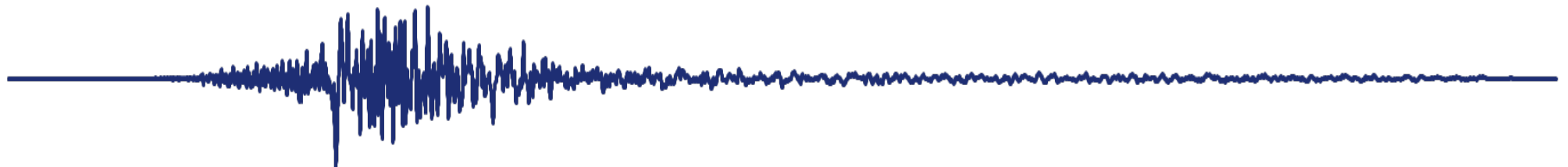
SHMC-6 GMM Sigma Values - $\sigma(x)$

Tectonic Regime	$\bar{\sigma}$ (PGA)
Crustal	0.590
In-Slab	0.676
Interface	0.692

Source: Earthquake Engineering Research Facility, UBC



Source: Kolaj et al. (2019). "Ground-motion models for the 6th Generation Seismic Hazard Model of Canada"



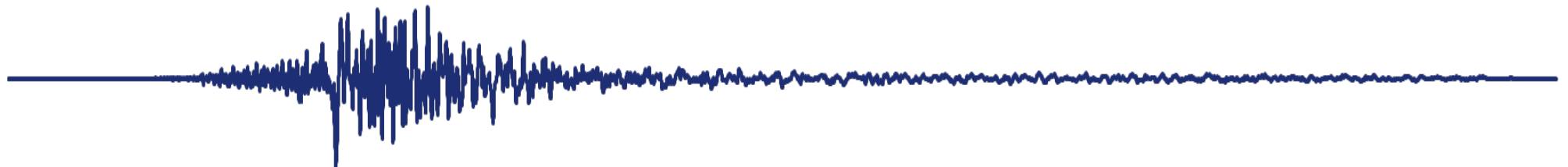
Median X from $\bar{\varepsilon}(x)$ and $\bar{\sigma}(x)$

$$\ln(\text{med_PGA}) = \mu = \ln(\text{PGA}_{2p50}) - \bar{\varepsilon}(\text{PGA}) \cdot \bar{\sigma}(\text{PGA})$$

From deaggregation of PGA = 0.580g at 2%/50-years ($V_{s30} = 1100$ m/s):

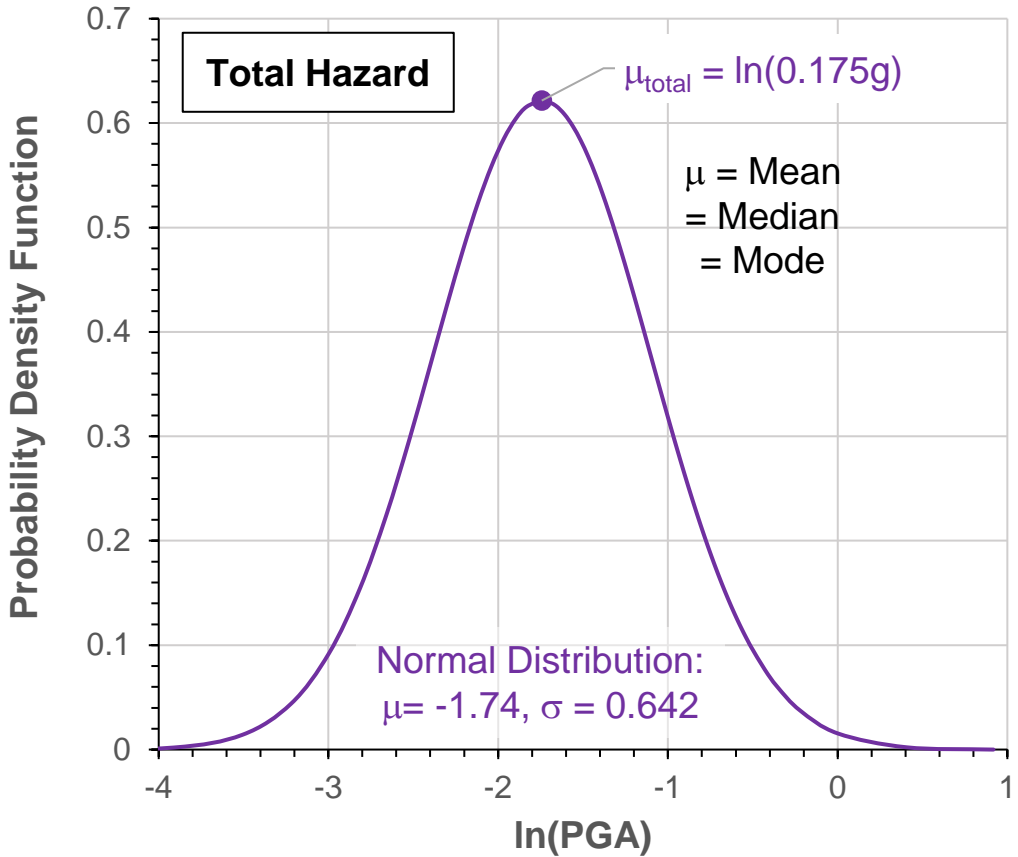
Tectonic Regime	Contribution	$\bar{\varepsilon}(\text{PGA})$	$\bar{\sigma}(\text{PGA})$	Median PGA (g)
Crustal	44%	1.51	0.590	0.240
In-Slab	33%	2.29	0.676	0.125
Interface	23%	1.96	0.692	0.150
Total Hazard	100%	1.87	0.642	0.175

$$\mu_{\text{total}} = \ln(0.175) = -1.74$$

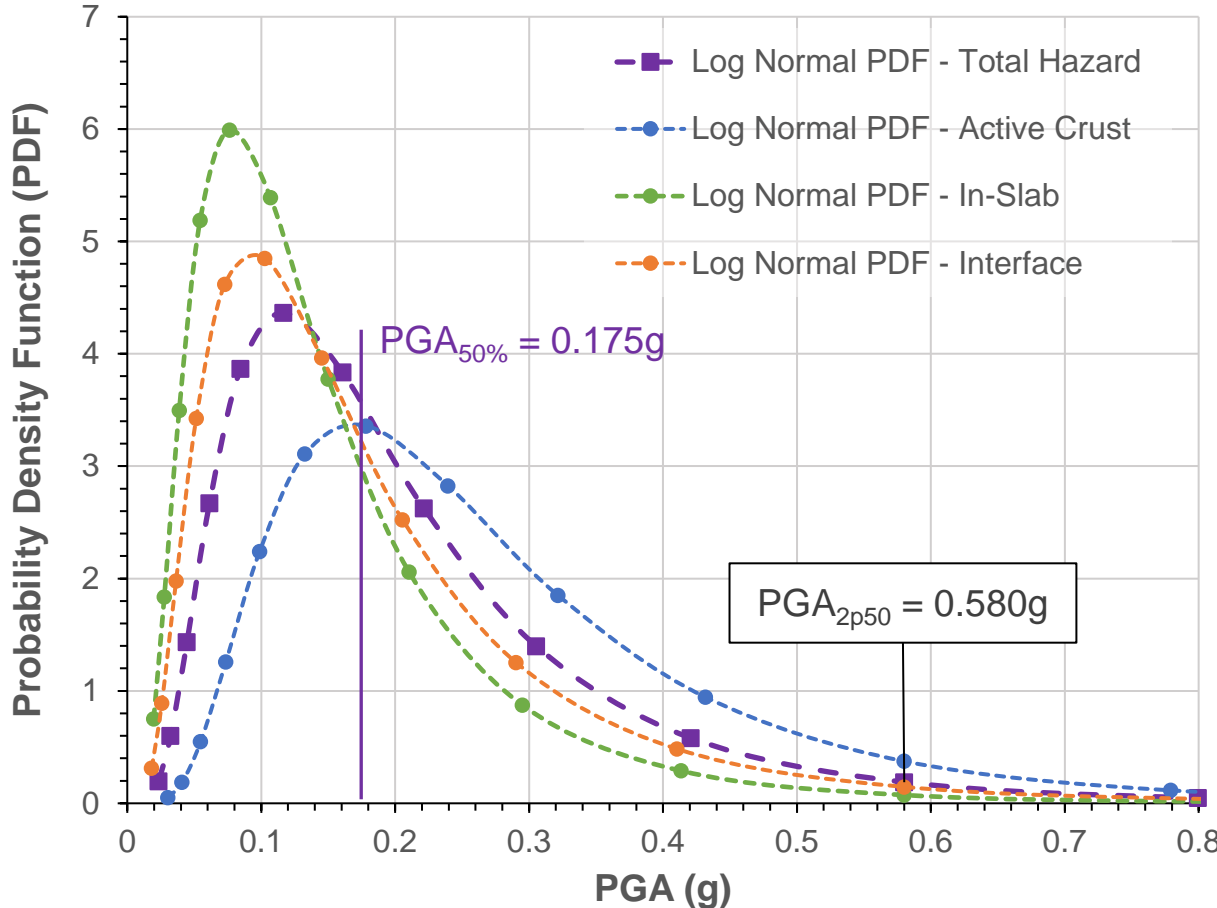



Probability Distribution of X from ε Distribution

Ln(PGA) Distribution from Deaggregation of PGA(X1100) at 2%/50-years

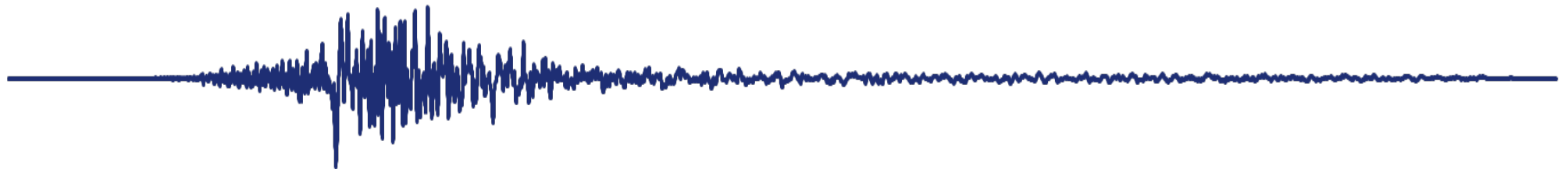
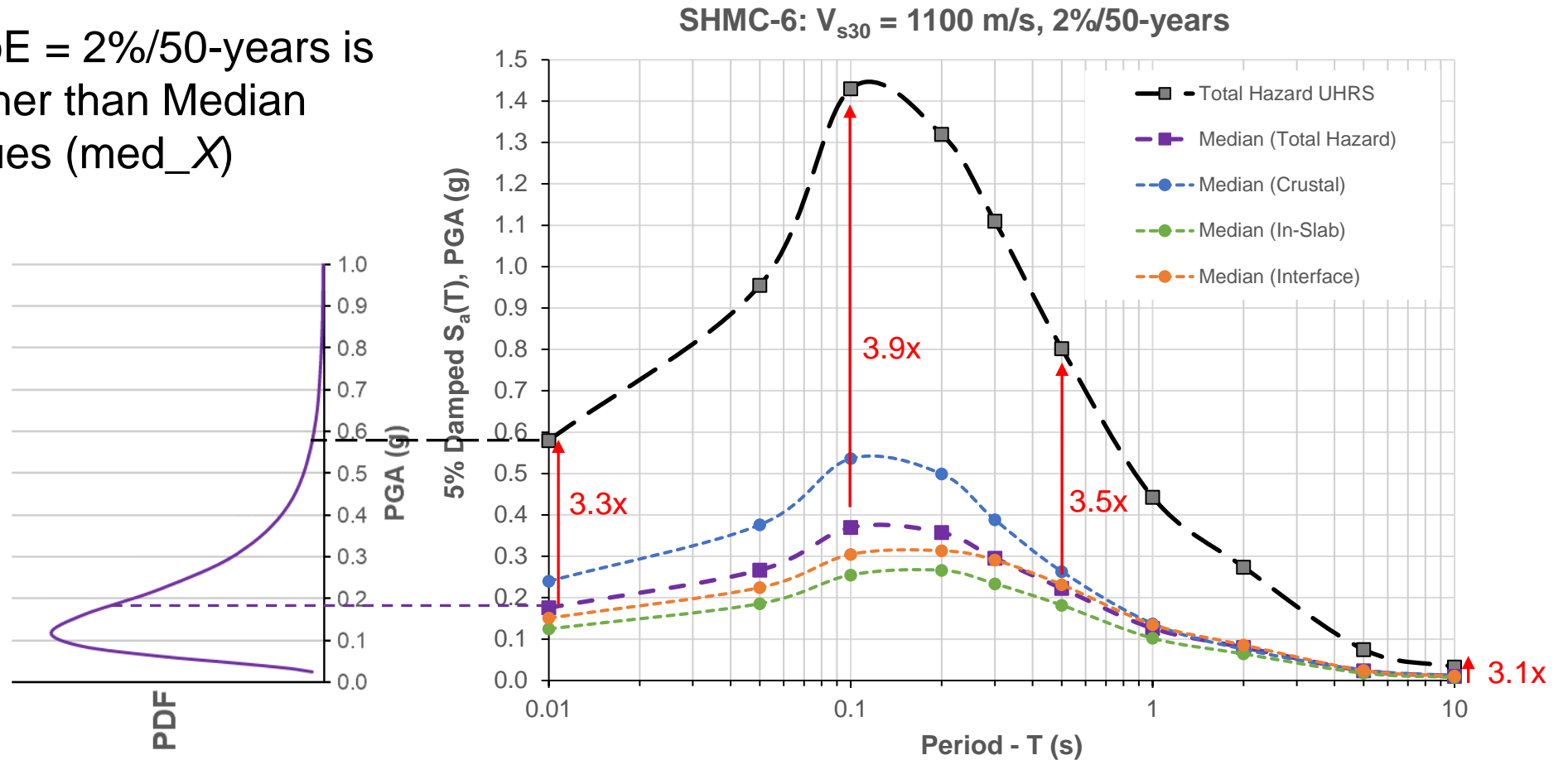


PGA Distribution from Deaggregation of PGA(X1100) at 2%/50-years



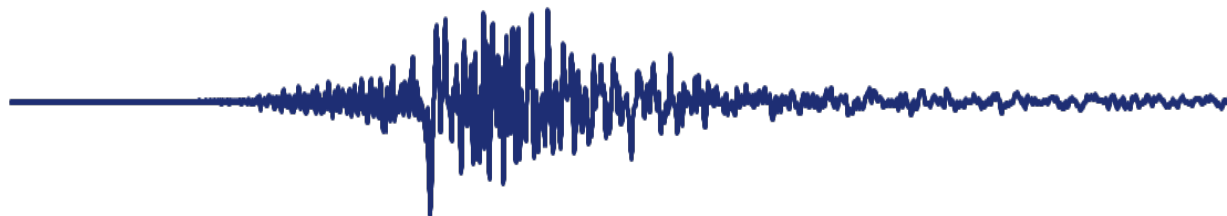
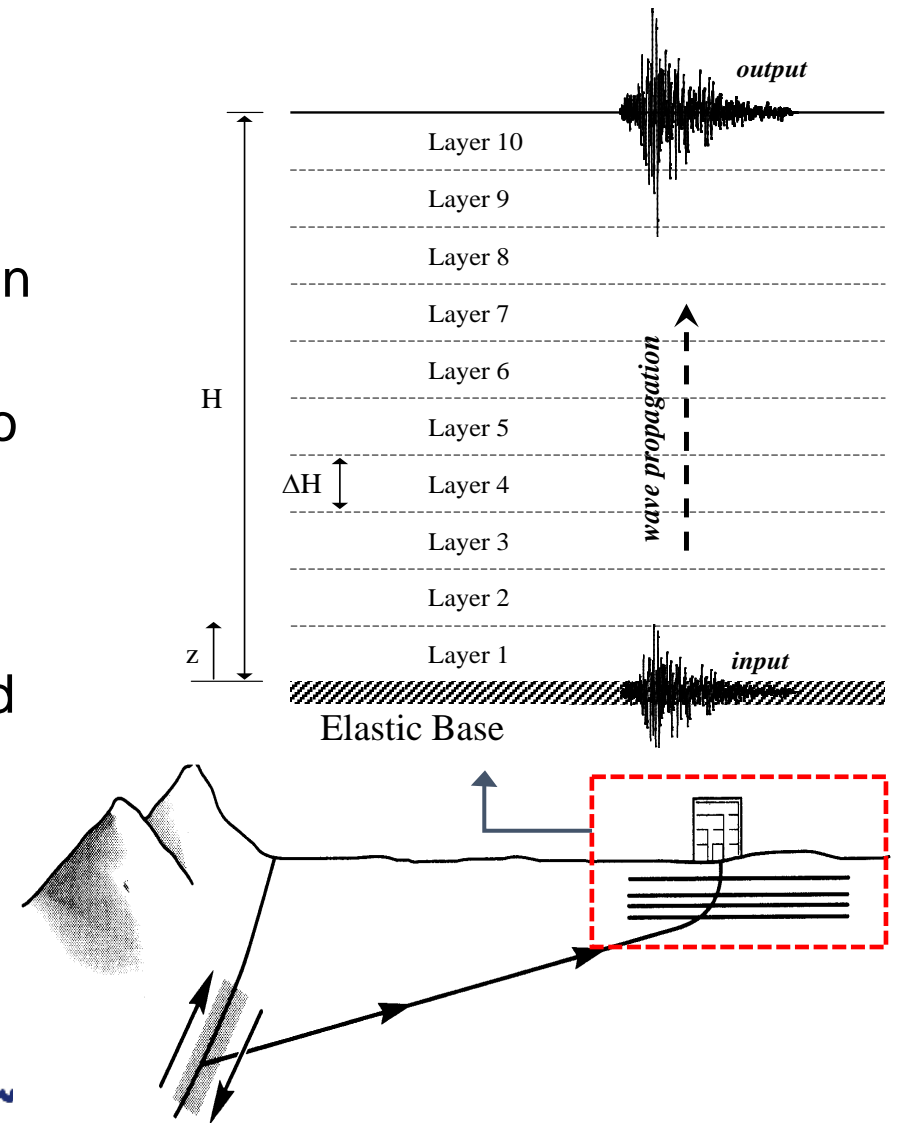
Median Response Spectrum vs UHRS

- UHRS at PoE = 2%/50-years is 3x to 4x higher than Median Hazard Values (med_X)



Seismic Site Response Analysis (SSRA)

- Models the response of a multi-layered soil profile to the upward propagation of horizontal shear waves during an earthquake – i.e. an individual event response
- Multiple analyses are run on suite(s) of horizontal acceleration time histories
- Acceleration time histories, $a(t)$, are scaled and/or matched to a target response spectrum for a reference ground condition that represents the conditions within a basal layer that behaves as an elastic material (ideally bedrock)
- Intensity and frequency content of the ground motions altered by dynamic soil properties that vary with shear strain (γ):
 - Shear stiffness (G) decreases with increasing γ
 - Hysteretic Damping (D) increases with increasing γ



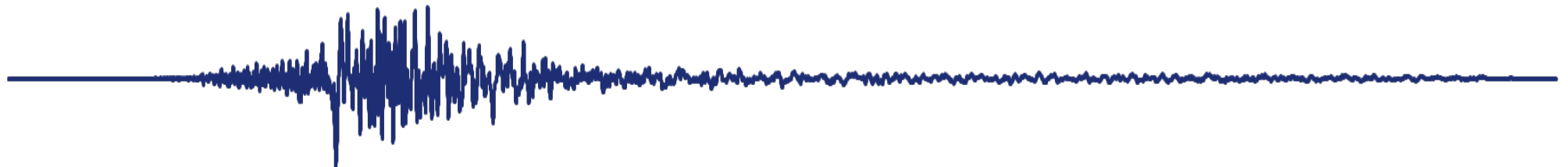
Calculating UHRS from SSRA (NBC 2015)

Typical Practice:

1. Scale and/or spectrally match individual event time histories to a probabilistic target UHRS of reference ground condition corresponding to aggregated hazard at design hazard level
2. Conduct deterministic SSRA to generate a suite of amplified response spectra
3. Use mean of amplified $S_a(T)$ for structural design
 - Amplified $S_a(T)$ at any T is depends on how well input $S_a(T)$ matches target $UHRS_{ref}$ at T
 - Amplification effects depend on non-linear soil behaviour; non-linearity increases with increasing shear strain; large shear strains induced by very high aggregated hazard values

Apply Amplification Function Using “Hybrid Method” (Stewart et al., 2014)

1. & 2. Same as above
3. For each time history, calculate $F(T) = S_a(T)_{out}/S_a(T)_{in}$
4. Amplified $S_a(T) = \text{Mean } F(T) \times \text{Target } UHRS_{ref}$
 - Consistent with $F(T)$ approach in NBC 2015
 - Non-linear amplification effects based on intensity of input motions scaled to target UHRS of aggregated hazard at design hazard level



NBC 2020-Consistent SSRA

- **Pilot Study** conducted by Thurber Engineering and the Earthquake Engineering Research Facility (UBC), peer review by Golder-WSP, funding by EGBC
- **Purpose:** To investigate how SSRA can be implemented within NBC 2020 framework for structural analysis of seismic retrofits for BC schools in accordance with the Seismic Retrofit Guidelines, 2020 Ed.
- **Objectives:**
 - To incorporate SSRA results directly within SHMC-6 allowing probabilistic computation of amplified UHRS – **Rigorous Method**
 - Compare amplified UHRS from rigorous method to **Simplified Methods** of calculating UHRS using SSRA results: *“Hybrid Method”* and *“Modified Hybrid Method”* described by Stewart et al. (2014)



PACIFIC EARTHQUAKE ENGINEERING
RESEARCH CENTER

Guidelines for Performing Hazard-Consistent
One-Dimensional Ground Response Analysis
for Ground Motion Prediction

Jonathan P. Stewart
Kioumars Afshari

Department of Civil and Environmental Engineering
University of California, Los Angeles

Youssef M.A. Hashash

Department of Civil and Environmental Engineering
University of Illinois, Urbana-Champaign

Project Review Panel:

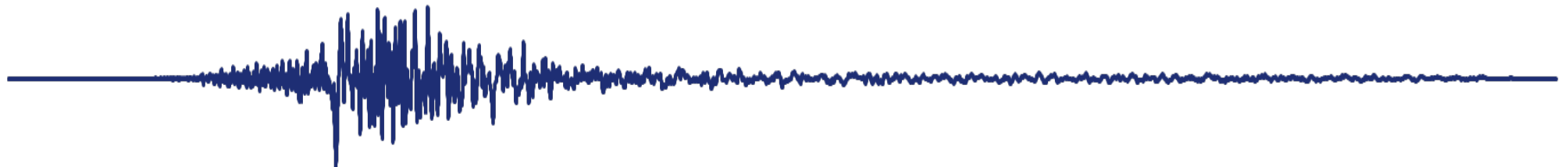
Thomas Shantz
Brian S.-J. Chiou

California Department of Transportation
Sacramento, California

Yousef Bozorgnia
Christine A. Goulet

Pacific Earthquake Engineering Research Center
Berkeley, California

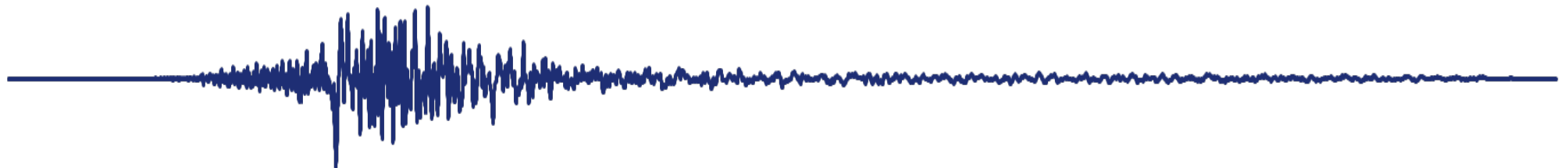
PEER 2014/16
OCTOBER 2014



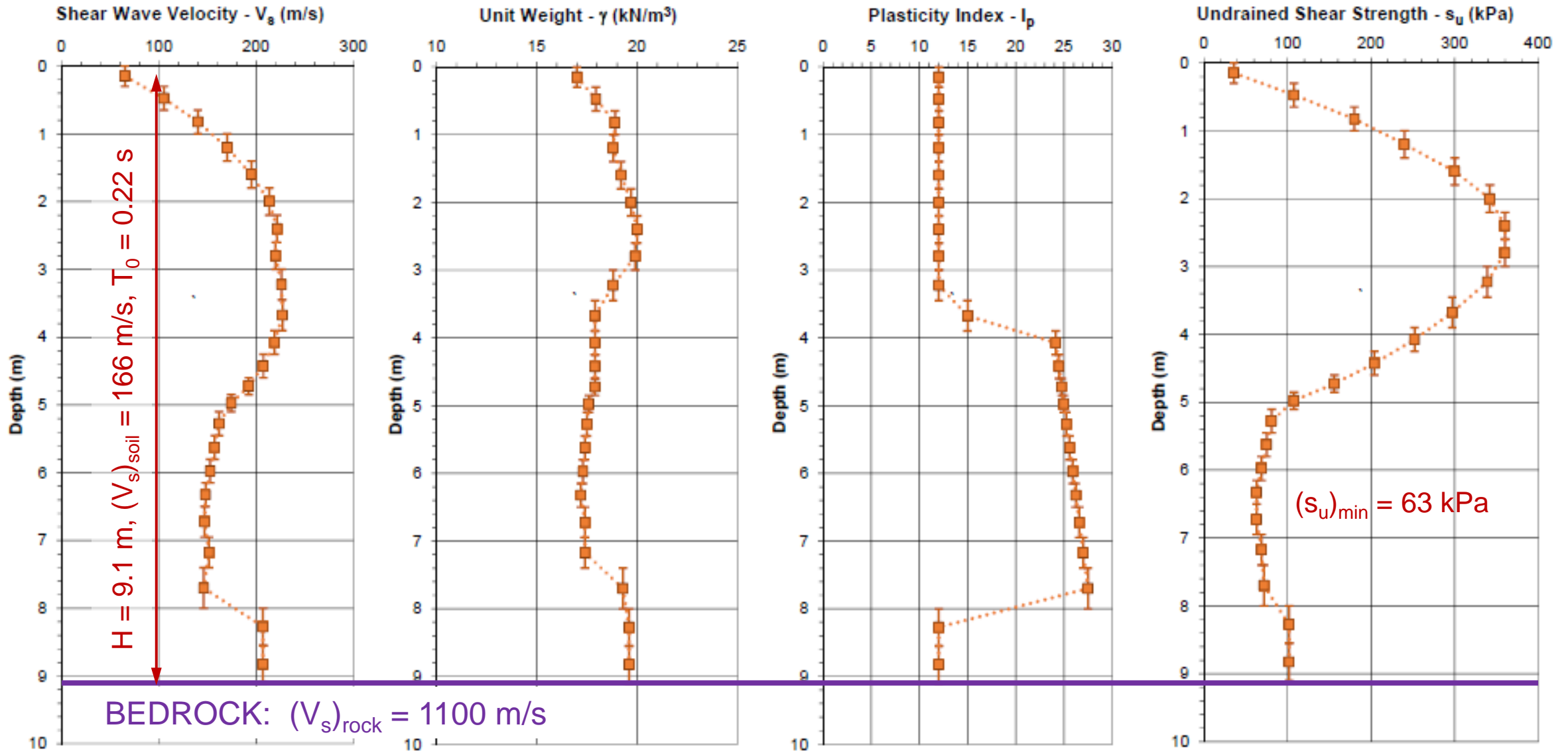
NBC 2020-Consistent SSRA: Pilot Study on SSRA in SRG 2020

Acknowledgments

- Thurber: McKenzie Douglas, Paul Wilson
- University of British Columbia EERF: Armin Bebamzadeh, Mike Fairhurst, Carlos Ventura
- Golder-WSP: Roberto Olivera
- Engineers & Geoscientists BC: Peter Mitchell
- Natural Resources Canada: Michal Kolaj, Stephen Halchuk
- Graham Taylor (TBG Seismic Consultants)
- Tuna Onur (Onur Seemann Consulting)



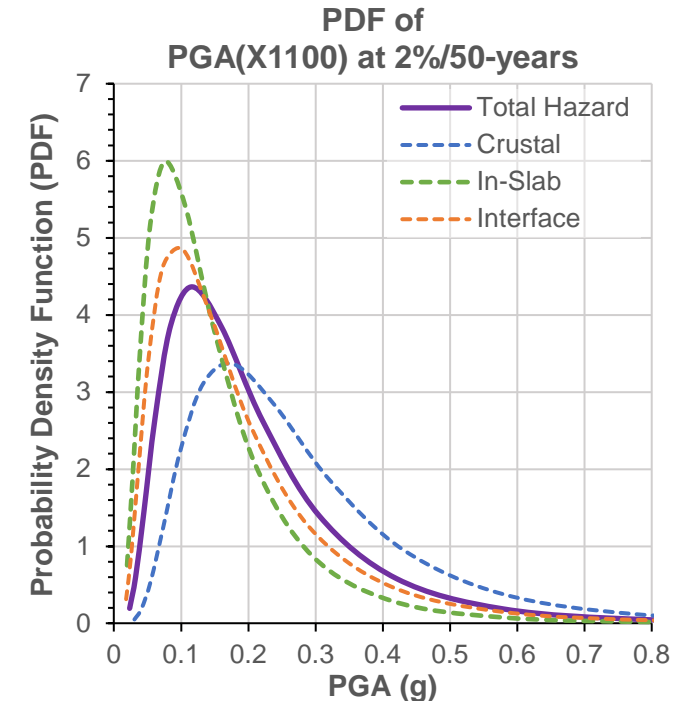
Test Site: Legislative Assembly of BC, Victoria



Calculating UHRS from SSRA (NBC 2020)

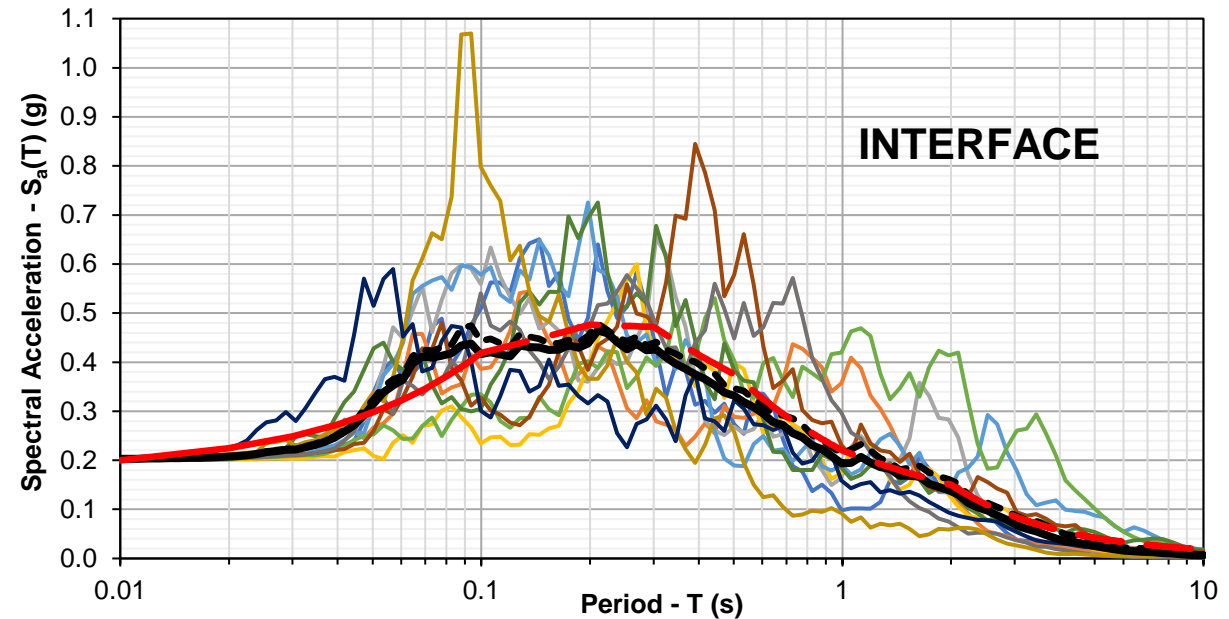
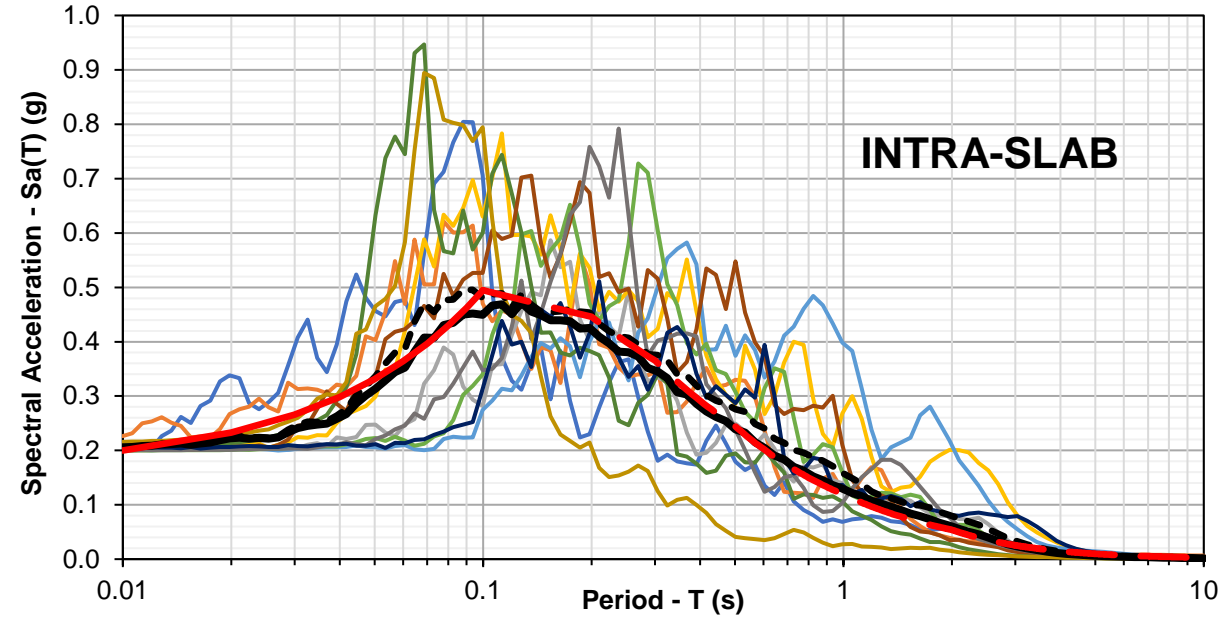
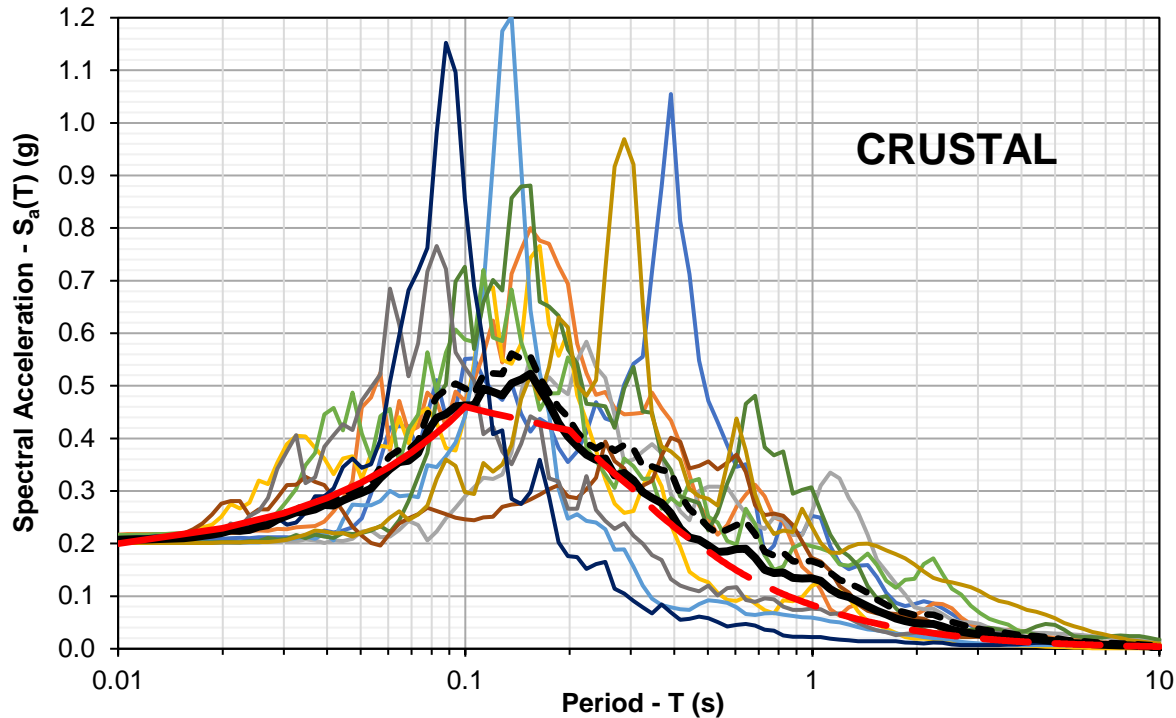
Rigorous Method Implemented in SSRA Pilot Study:

1. Scale earthquake acceleration time histories to various PGA_{ref} corresponding to the range of median PGA_{ref} for individual event scenarios within the hazard model
2. Conduct deterministic SSRA to generate suites of $F(T, PGA_{ref})$ for each Tectonic Regime Type (TRT)
3. Replace site terms in the GMMs with lookup tables of mean $F(T, PGA_{ref})$ for each tectonic source
4. Hazard model computes amplified $S_a(T)$ for each event scenario as a function of $F(T, PGA_{ref})$ and the GMM-predicted median PGA_{ref} , then probabilistically aggregates the amplified $S_a(T)$ to generate hazard curves for each T
5. Construct the UHRS at hazard level of interest using the hazard curves



Input Response Spectra (Ref $V_{s30} = 1100$ m/s)

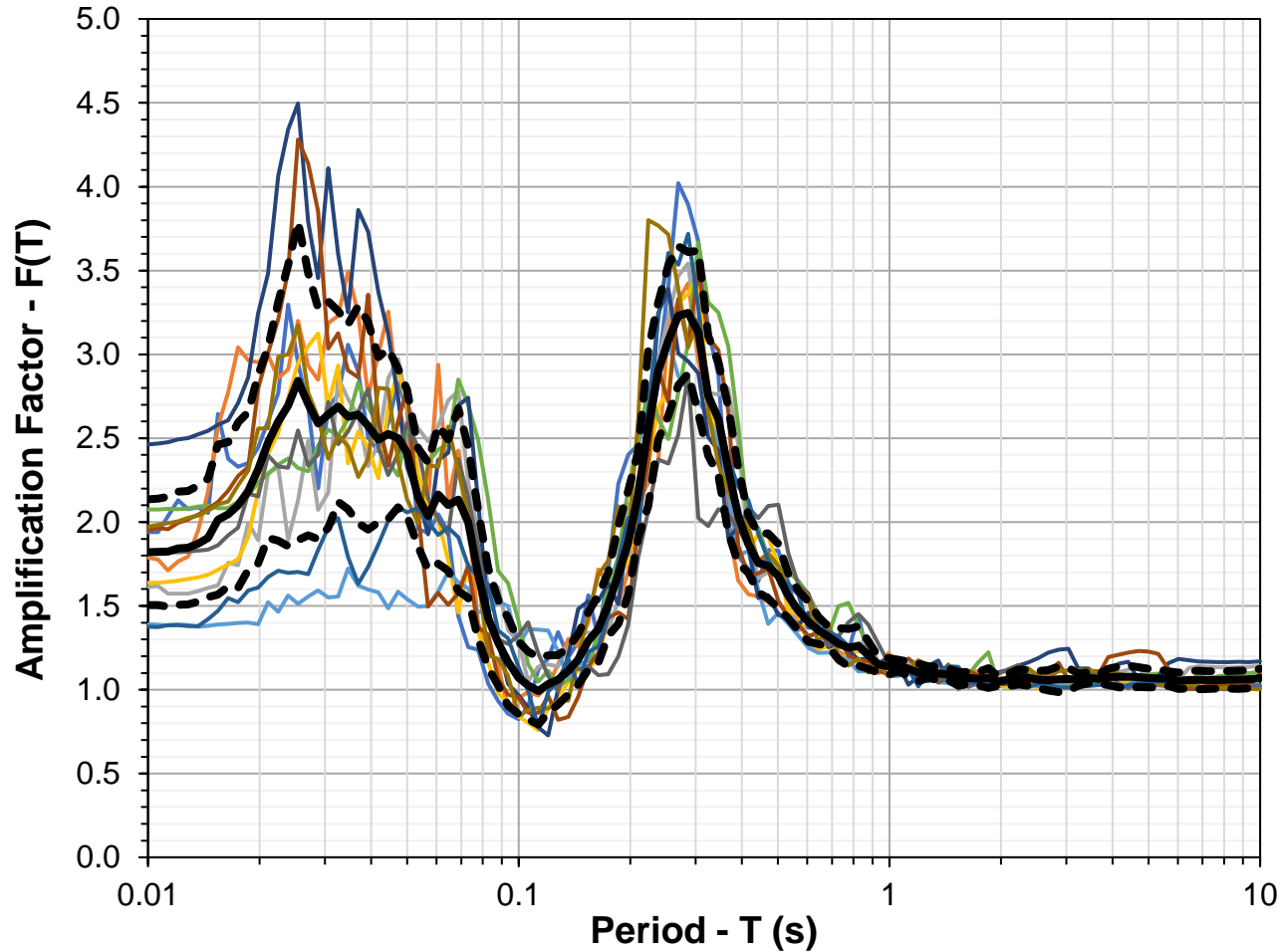
- Target Response Spectra: 2%/50yrs UHRS for each TRT from SHMC-6:
Crustal, Intra-Slab, Interface
- Suites of 11 EQ records for each TRT selected by UBC scaling for best fit of $S_a(T)$ geomean to target
- Each suite scaled to multiple intensity levels:
 $PGA_{ref} = 0.05g, 0.10g, 0.20g, 0.40g, 0.60g$



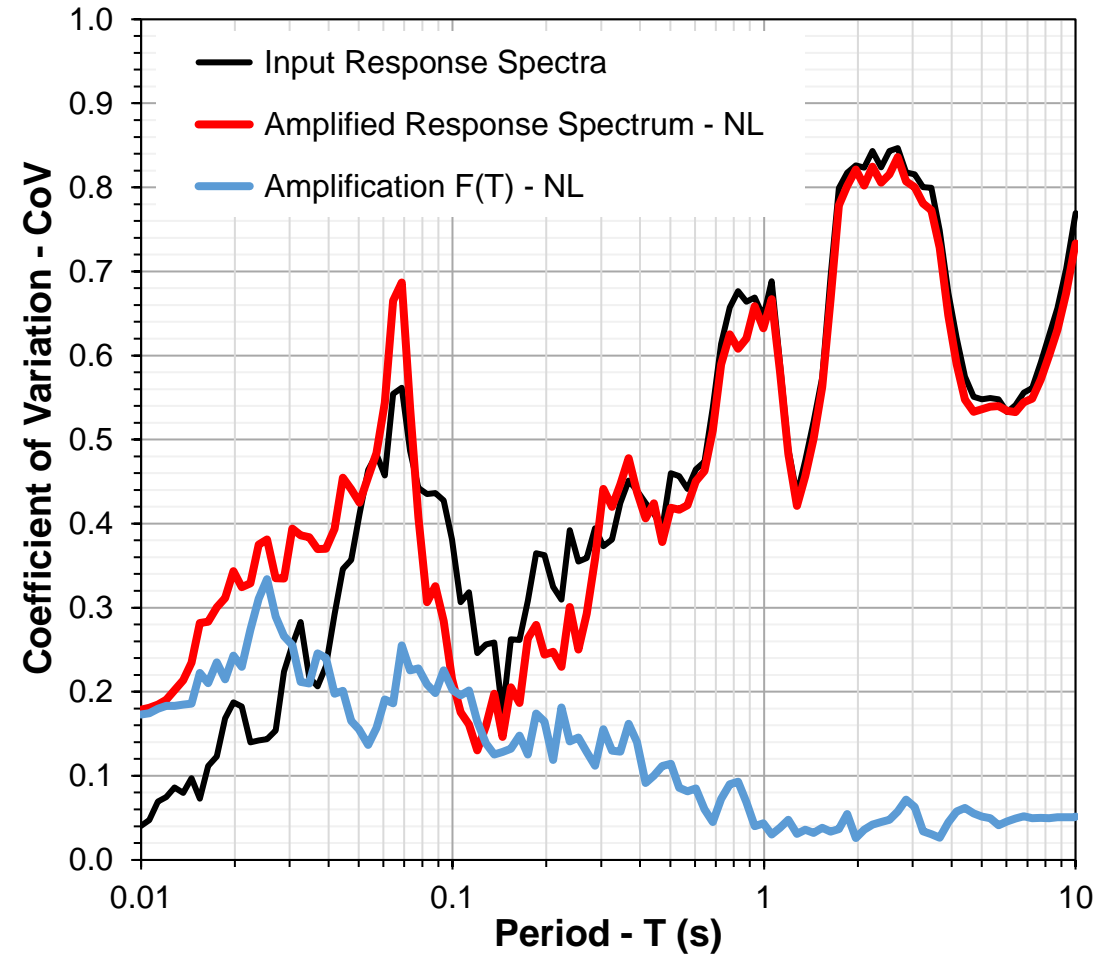
Amplification Function - $F(T, PGA_{ref})$

At each PGA_{ref} , $F(T)_j = S_a(T)_{output} / S_a(T)_{input}$

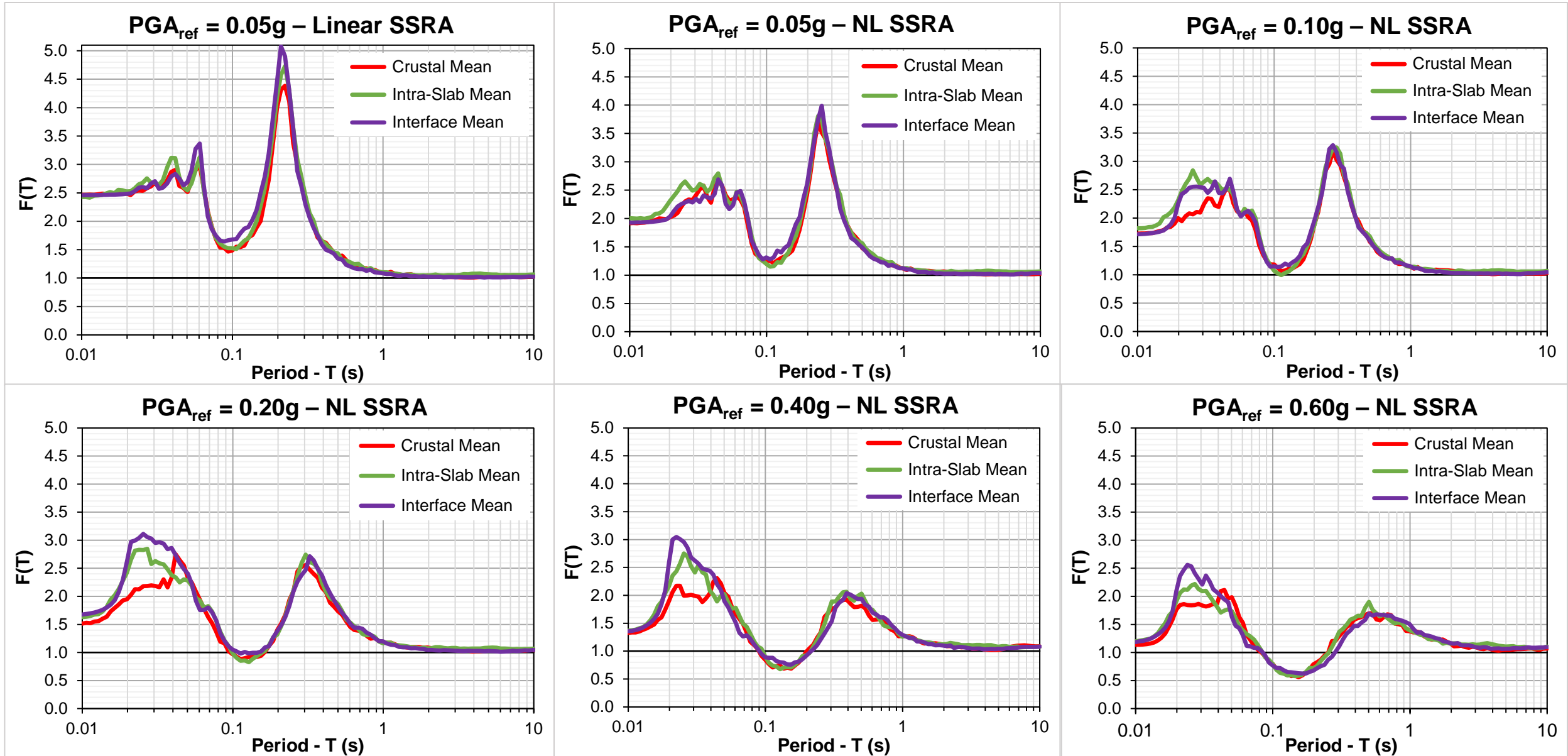
Non-Linear SSRA: Intra-Slab at $PGA_{ref} = 0.10g$



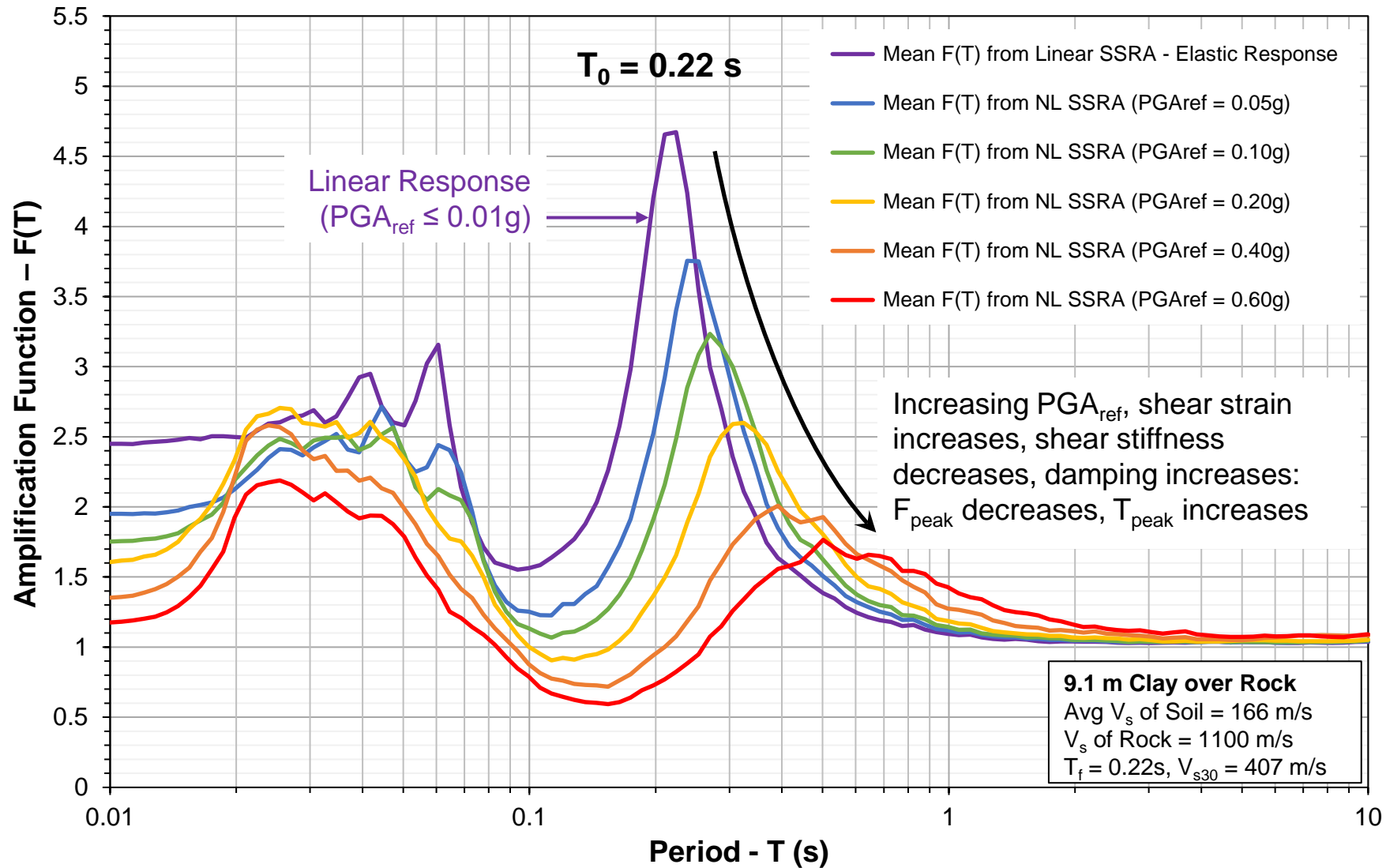
Intra-Slab at $PGA_{ref} = 0.10g$



Mean $F(T, PGA_{ref})$ from SSRA

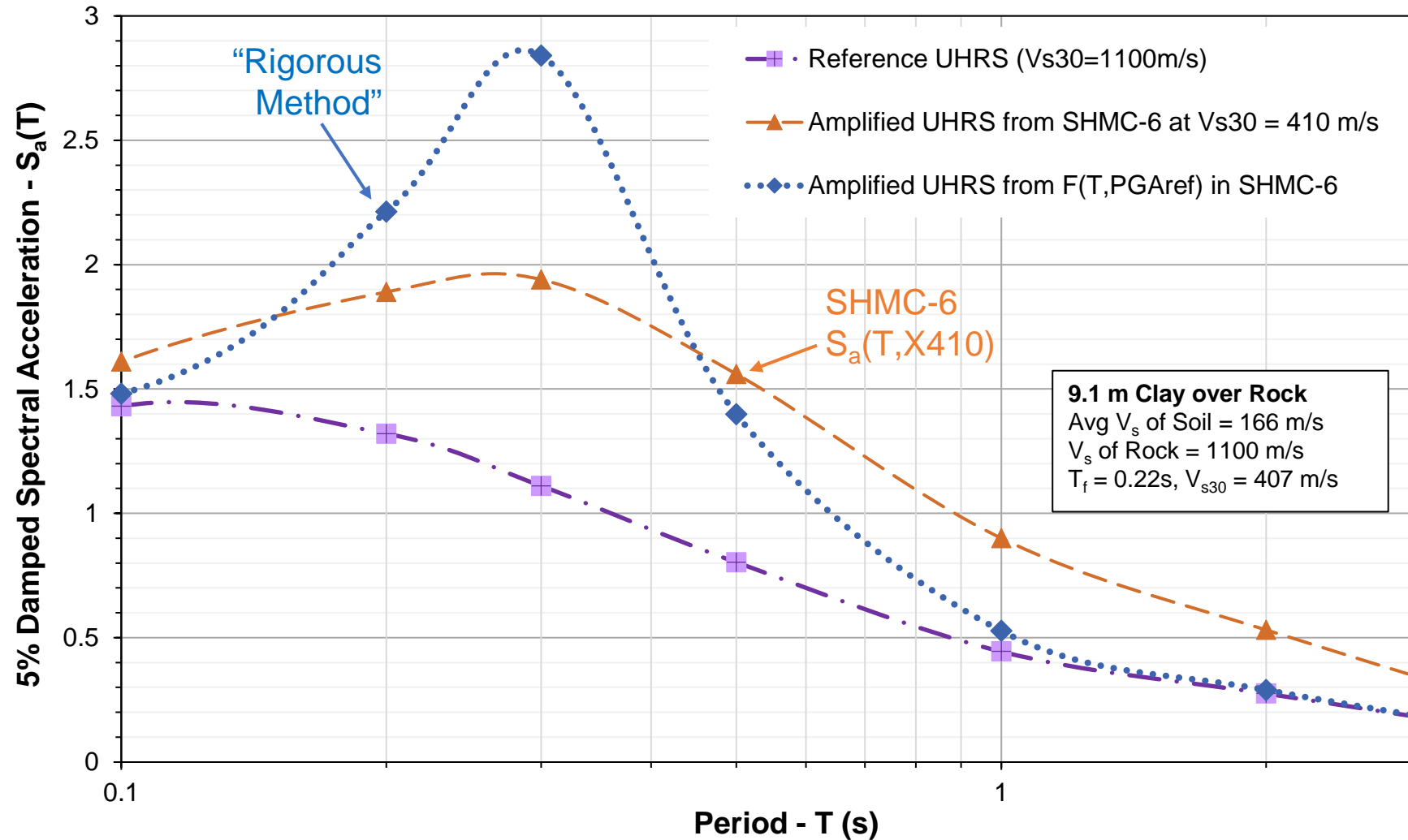


Mean $F(T, PGA_{ref})$ from SSRA (All TRT)



UHRS from $F(T, PGA_{ref})$ in SHMC-6 (Rigorous Method)

UHRS at 2% in 50 years P.E.



Calculating UHRS from SSRA (NBC 2020)

Simplified Method - “Modified Hybrid” Method (Stewart et al. 2014):

$$\text{Amplified } S_a(T) = F(T, \text{Med_PGA}_{\text{ref}}) \times \text{UHRS}_{\text{ref}}$$

- Median PGA_{ref} calculated using mean epsilon ($\bar{\epsilon}$) from deaggregation of PGA_{ref} at hazard level of interest (e.g. 2%/50-years) and tectonic source-weighted mean sigma ($\bar{\sigma}_{\text{Total}}$):

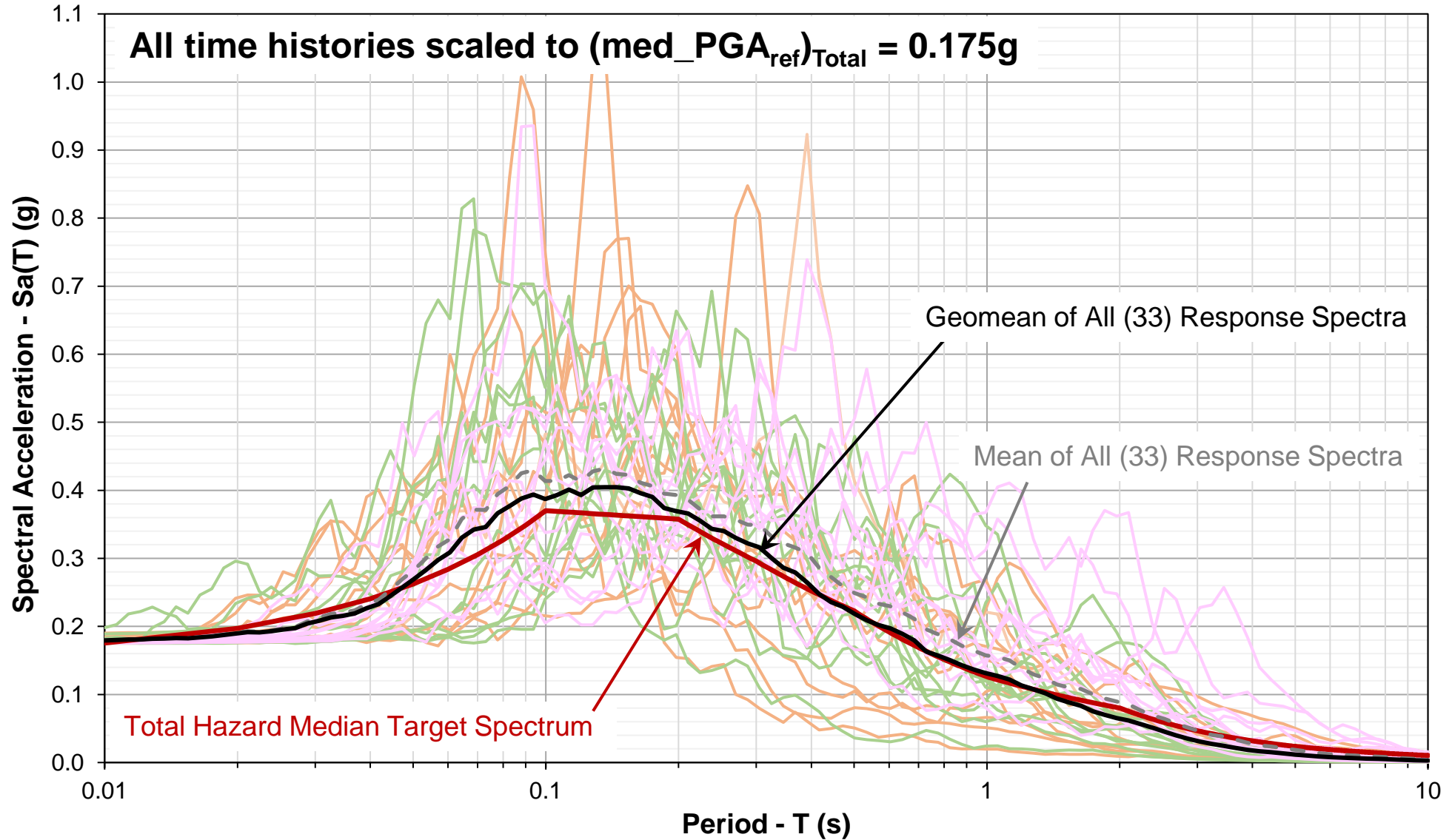
$$\text{eg. } \ln(\text{Med_PGA}_{\text{ref}}) = \ln(\text{PGA}_{\text{ref_2p50}}) - \bar{\epsilon}_{2p50} \cdot \bar{\sigma}_{\text{Total}}$$

- $F(T, \text{Med_PGA}_{\text{ref}})$ calculated from SSRA using time histories scaled so $\text{PGA}_j = \text{Med_PGA}_{\text{ref}}$

From deaggregation of $\text{PGA} = 0.580\text{g}$ at 2%/50-years ($V_{s30} = 1100 \text{ m/s}$):

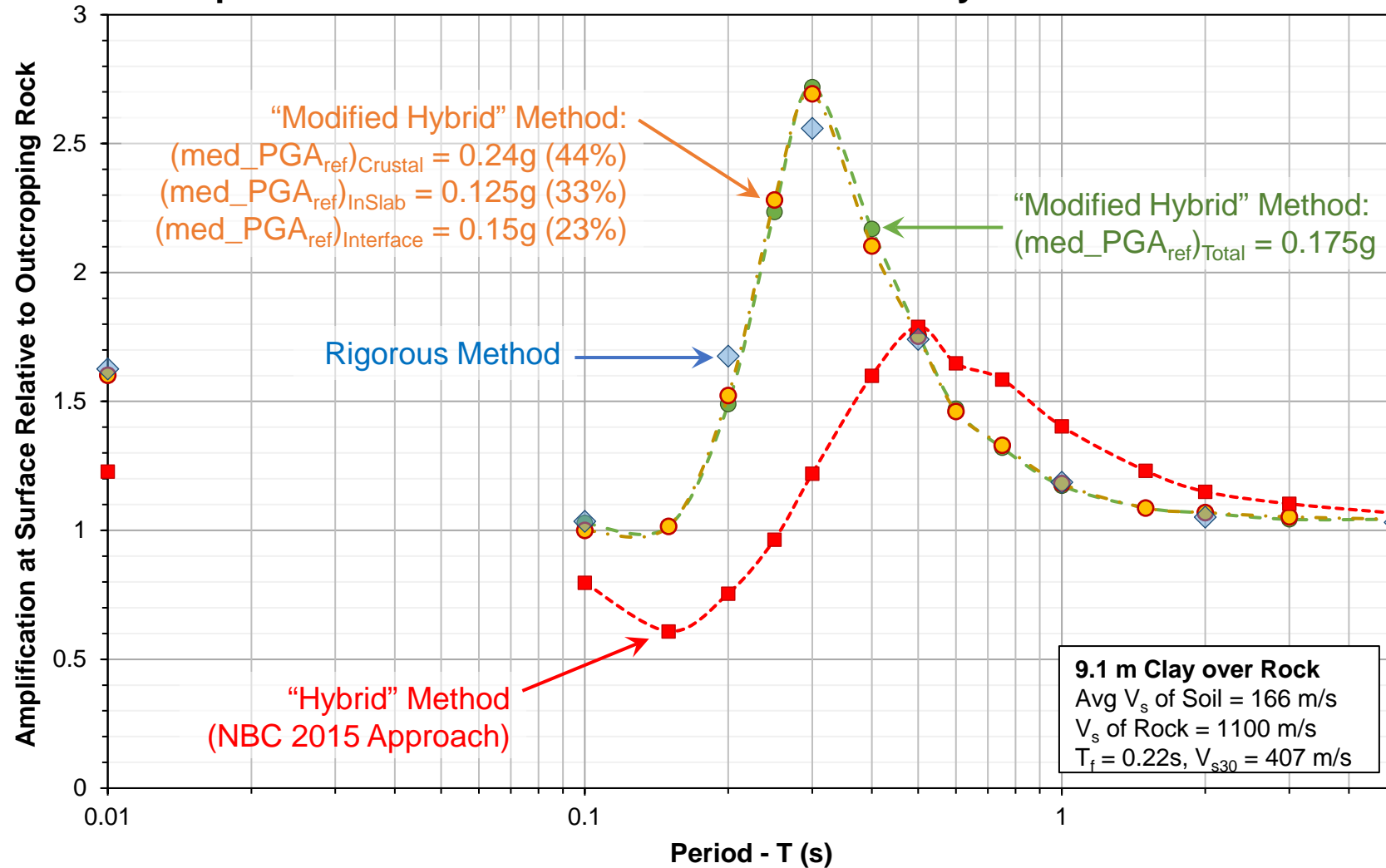
Tectonic Regime	Contribution	$\bar{\epsilon}(\text{PGA})$	$\bar{\sigma}(\text{PGA})$	Median PGA (g)
Crustal	44%	1.51	0.590	0.240
In-Slab	33%	2.29	0.676	0.125
Interface	23%	1.96	0.692	0.150
Total Hazard	100%	1.87	0.642	0.175

“Modified Hybrid” Method – Input Time History Scaling



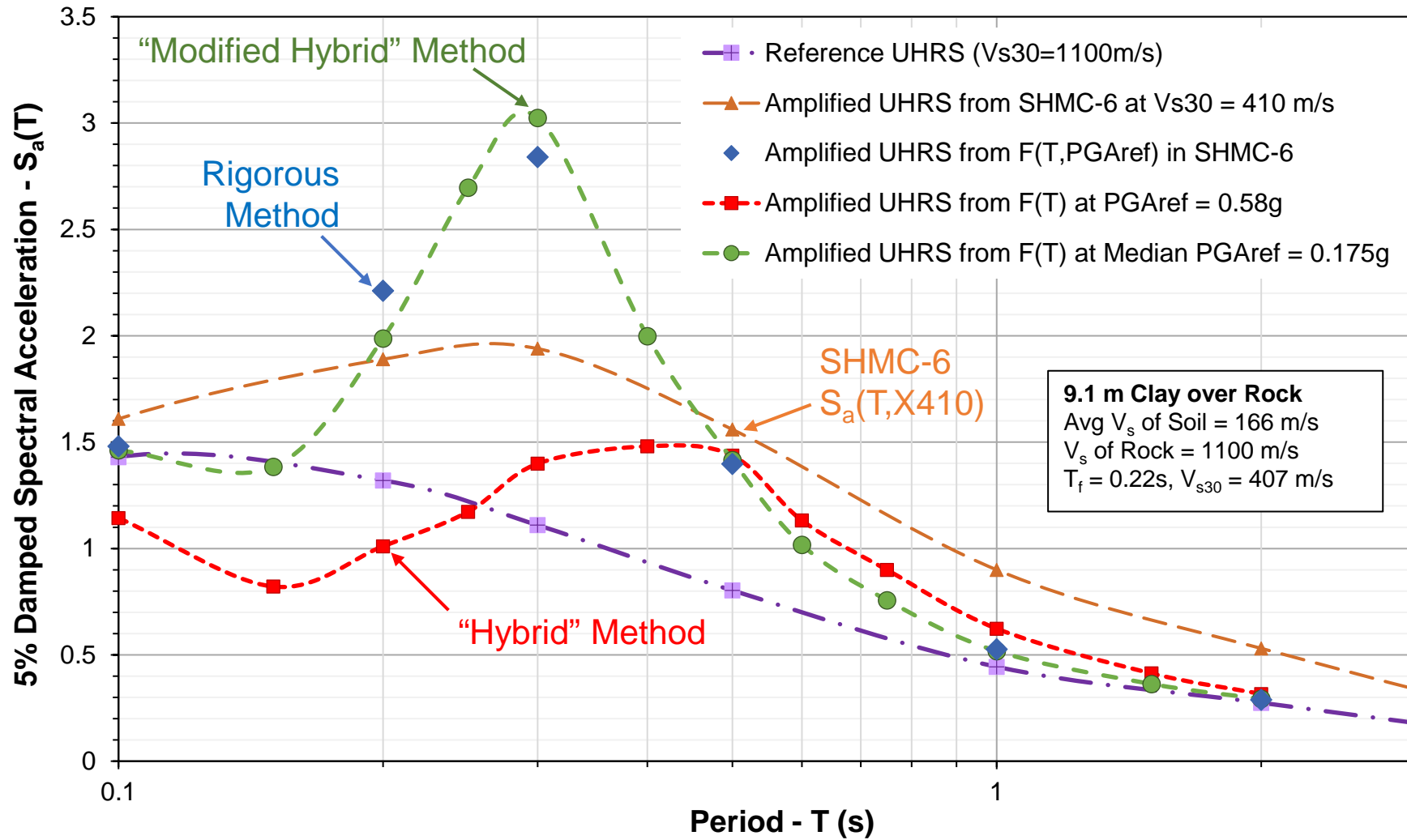
Mean F(T) from Rigorous & Simplified Methods

Amplification Functions from 1D SSRA - 2%/50-years Hazard Level



UHRs from Rigorous & Simplified Methods

UHRs at 2% in 50 years P.E.



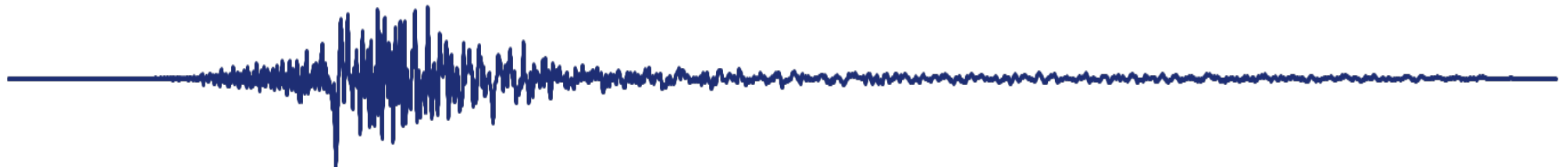
Summary - NBC 2020 vs NBC 2015 Amplification

NBC 2015

- $F(T, PGA_{ref})$ for each Site Class provided in the code
- PGA_{ref} (= PGA_C in Western Canada) is the “intensity measure” used to model non-linear response
- PGA_C is a probabilistic hazard value on the aggregated hazard curve
- Since $PGA_C \gg PGA_i$ of individual event scenarios, $F(T, PGA_{ref})$ for high PGA_{ref} tends to overpredict non-linearity and damping and so underpredicts non-linear amplification

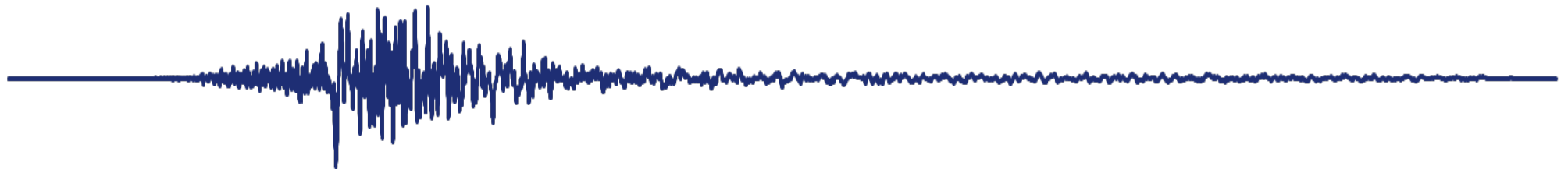
NBC 2020

- Each GMM uses site terms to estimate amplification of rock ground motion values predicted for individual event scenarios within SHMC-6
- Linear amplification relative to a rock reference condition calculated based on V_{s30} of site
- Non-linear amplification is a function of the median prediction of a short-period intensity measure for the reference condition (typ. PGA_{rock}) at the event scenario level
- Amplified hazard values for each event scenario are probabilistically aggregated



Summary – NBC 2020-Compatible SSRA

1. Reference Ground Condition – assign X_v consistent with elastic basal layer in analysis
2. Median Target Spectrum for reference condition at design hazard level - construct using suite of site-specific deaggregation data for X_v at design hazard level: $\ln(\text{med_}x_{\text{ref}}) = \ln(X_{\text{ref}}) - \bar{\varepsilon}(x_{\text{ref}}) \cdot \bar{\sigma}(x)$
3. Time History Selection – scale TRT-relevant time histories to $(\text{med_PGA}_{\text{ref}})_{\text{TRT}}$; geomean of suite should be close to target spectrum for each TRT
4. Input Time Histories: i) TRT-specific suite scaled to $(\text{med_PGA}_{\text{ref}})_{\text{TRT}}$; or ii) All time histories scaled to $(\text{med_PGA}_{\text{ref}})_{\text{Total}}$
5. Run SSRA and calculate $F(T)_j = S_a(T)_{\text{out}}/S_a(T)_{\text{in}}$ for each time history
6. Mean Amplification Function: $\bar{F}(T)_{\text{Total}} = \sum c_{\text{TRT}} \cdot \bar{F}(T)_{\text{TRT}}$, where c_{TRT} is % contribution of each TRT, $\bar{F}(T)_{\text{TRT}}$ is mean (conservative) or geomean of all $F(T)_j$ in the TRT-specific suite
7. Amplified UHRS at design hazard level: $S_a(T) = \bar{F}(T)_{\text{Total}} \cdot S_a(T)_{\text{ref}}$



Questions?

